A BRIEF REVIEW OF AQ LEARNING PROGRAMS AND THEIR APPLICATION TO THE MONKS' PROBLEMS:

J. Bala, E. Bloedorn, K. De Jong, K. Kaufman, R.S. Michalski, P. Pachowicz, H. Vafaie, J. Wnek and J. Zhang

Center for Artificial Intelligence George Mason University

Abstract

This paper describes results from applying various AQ learning programs to the Monks' problems. The Monks' problems are concerned with learning concept descriptions from examples, and were developed by Sebastian Thrun and John Cheng at the 1991 European Summer School on Machine Learning at the Priory Corsendonk in Oud Turnhout, Belgium. All examples come from the same event space, which spans 6 multiple-valued attributes, giving a total of 432 possible events.

The problems differ in terms of the type of the target concept to be learned, and in the amount of noise in the data. The target concept in the first problem includes a condition of whether or not two of the attributes have equal values. The target concept in the second problem is based on the number of attributes that have a designated value. The third problem presented a simple concept in which 10% of the training examples were noise.

The rules produced by the AQ programs for classifying the testing examples on these problems had error rates of no more than 13.2%, and for each of the three problems, at least one of the AQ programs achieved 100% correct classification.

1. INTRODUCTION

There have been a number of learning methods and approaches developed for inductive concept learning from examples. These methods can be divided into symbolic and subsymbolic, based on whether or not their representations of attributes and concepts consist of simple symbolic structures (e.g. logical descriptions) that can be related directly to the objects they represent. Typical symbolic representations include decision trees or rules, while subsymbolic methods include genetic algorithms and neural networks.

Given the many machine learning programs that have been developed for the purpose of concept learning, an important theoretical and practical problem is to determine the areas of best applicability of the various methods. One of the efforts in this direction was an international competition in which attendees at the 1991 European Summer School on Machine Learning were challenged with three problems developed by Thrun and Cheng (Thrun et al, 1991). Given that the School was being held on the grounds of a converted priory, the problems became known as the "Monks' Problems."

This paper describes the results from applying various AQ learning programs to these problems. The results of the application of other programs to these problems and a more brief presentation of the results using the AQ programs were documented by Thrun et al. (1991).

2. DATA FORMAT AND PROBLEM DEFINITIONS

The domain of the Monks' problems was an abstraction of a robots domain previously used in a comparison of learning methods' performance [Wnek et al, 1990]. The problems were presented in a way such that physical attributes and values were replaced by generic attributes and numerical values, for example, x1 is 2 instead of head_shape is square. In this paper, we will often revert to the latter notation or hybrid notation (such as head_shape is 2) when it makes the presentation more understandable. A complete listing of the attributes and values in both formats is shown in Table 1. All examples come from this event space, which spans 6 multiple-valued attributes (it has a total of 432 possible examples). The sizes of the value sets of the attributes, x1, x2, ..., x6, are 3, 3, 2, 3, 4, and 2, respectively.

Attribute Robot Att.	x1 head shape	x2 body shape	x3 is smiling	x4 holding	x5 jacket color	x6 has tie
	neua_srupe	bouy_snupe	ra_americang	The table	Jacitos_0010.	
Value				1929	_	
1	round	round	yes	sword	red	yes
2	square	square	no	balloon	yellow	no
3	Charles contro	octagon		flag	green	
3	octagon	OCIABOII		шь	•	
4					blue	

Table 1. Attributes and values in the robots domain

Problem 1.

There were 124 training examples, which represented 30% of the total event space (62 positive and 62 negative). The testing examples were all possible examples (216 positive and 216 negative). The goal concept was as follows:

This problem represented a straightforward concept in which the values of two attributes had to be compared, either implicitly or explicitly.

A diagrammatic visualization of this problem is shown in Figure 1. The dark area in this figure represents the positive concept, and the white area represents the concept negation, or the set of all possible counterexamples. Positive and negative training examples are represented by + and - respectively.

Problem 2.

There were 169 training examples, which represented 40% of the total event space (105 positive and 64 negative). The testing examples were all possible examples (190 positive and 242 negative). The goal concept was as follows:

Exactly two of the six attributes have their first value

In other words, exactly two of the x_i have values of 1. This concept does not have a simple representation in Disjunctive Normal Form, and therefore poses a problem for many symbolic learning methods.

A diagrammatic visualization of this problem is shown in Figure 2.

Problem 3.

There were 122 training examples, which represented 30% of the total event space (62 positive and 60 negative). The testing examples were all possible examples (204 positive and 228 negative). Noise was inserted into the example set so that 5% of the examples were misclassified. The goal concept was as follows:

```
(jacket_color is green and holding is sword) or (jacket_color is not blue and body_shape is not octagon)
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The goal of this problem was to test learning programs' adaptation to noisy environments.

A diagrammatic visualization of this problem is shown in Figure 3. The plus in the white area and the minuses in the black area represent the noisy training examples.

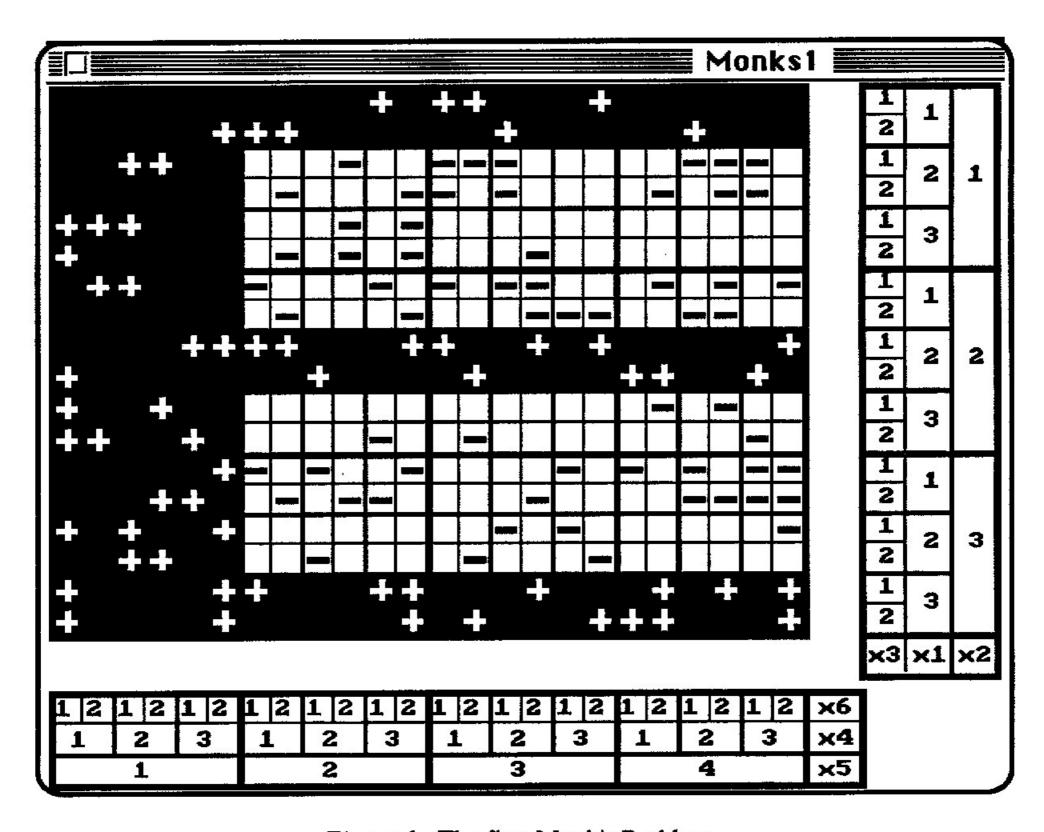


Figure 1. The first Monk's Problem

3. A BRIEF DESCRIPTION OF THE PROGRAMS AND ALGORITHMS

The following AQ programs were used in the experiments:

- AQ17-DCI (a version of AQ program with data-driven constructive induction)
- AQ15-FCLS (a version of AQ program oriented toward learning flexible concepts)
- AQ17-HCI (a version of AQ program with hypothesis-driven constructive induction)
- AQ14-NT (a version of AQ program oriented toward learning from noisy data)
- AQ15-GA (a version of AQ program combined with a genetic algorithm)

Below is a brief description of the algorithm AQ underlying all the problems, and then a description of each program.

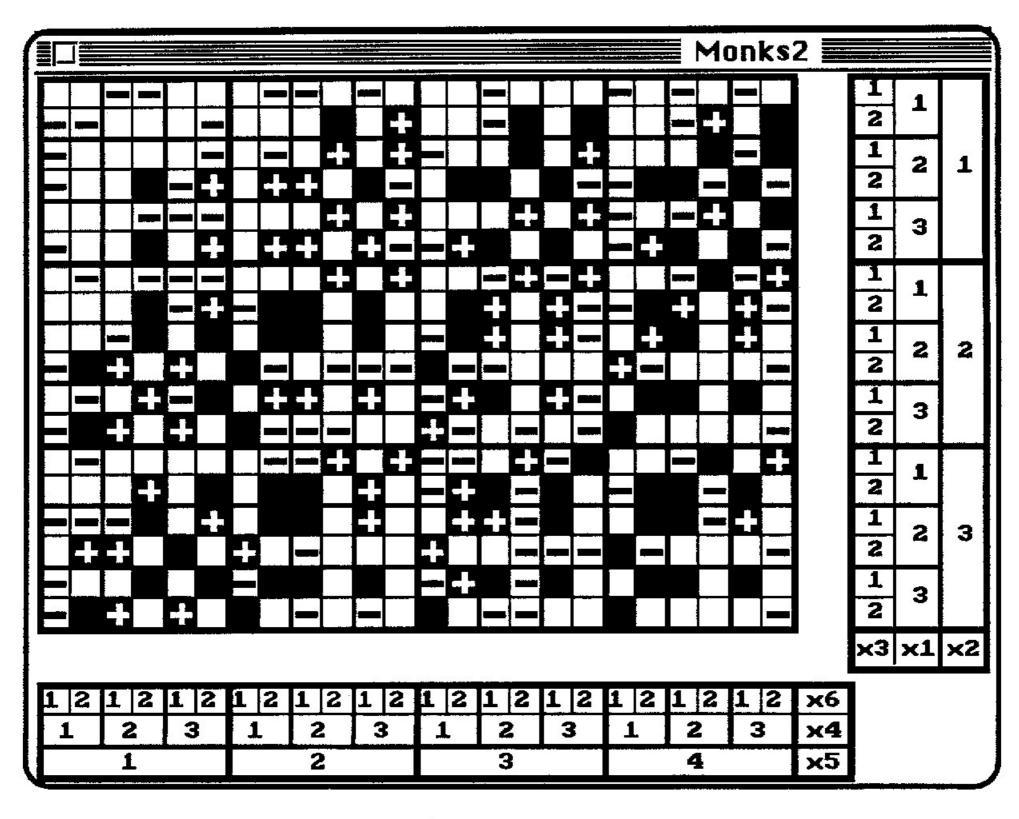


Figure 2. The second Monk's Problem

3.1. AQ Algorithm

All the above programs use AQ as the basic induction algorithm (Michalski, 1969; 1983). Here is a brief description of the AQ algorithm:

- 1. Select a seed example from the set of training examples for a given decision class.
- 2. Using the extend against operator (Michalski, 1983), generate a set of alternative most general rules (a star) that cover the seed example, but do not cover any negative examples of the class.
- 3. Select the "best" rule from the star according to a multi-criteria rule quality function (called LEF the lexicographical evaluation function), and remove the examples covered by this rule from from the set of positive examples yet to be covered.
- 4. If this set is not empty, select a new seed from it and go to step 2. Otherwise, if another decision class still requires rules to be learned, return to step 1, and perform it for the other decision class.

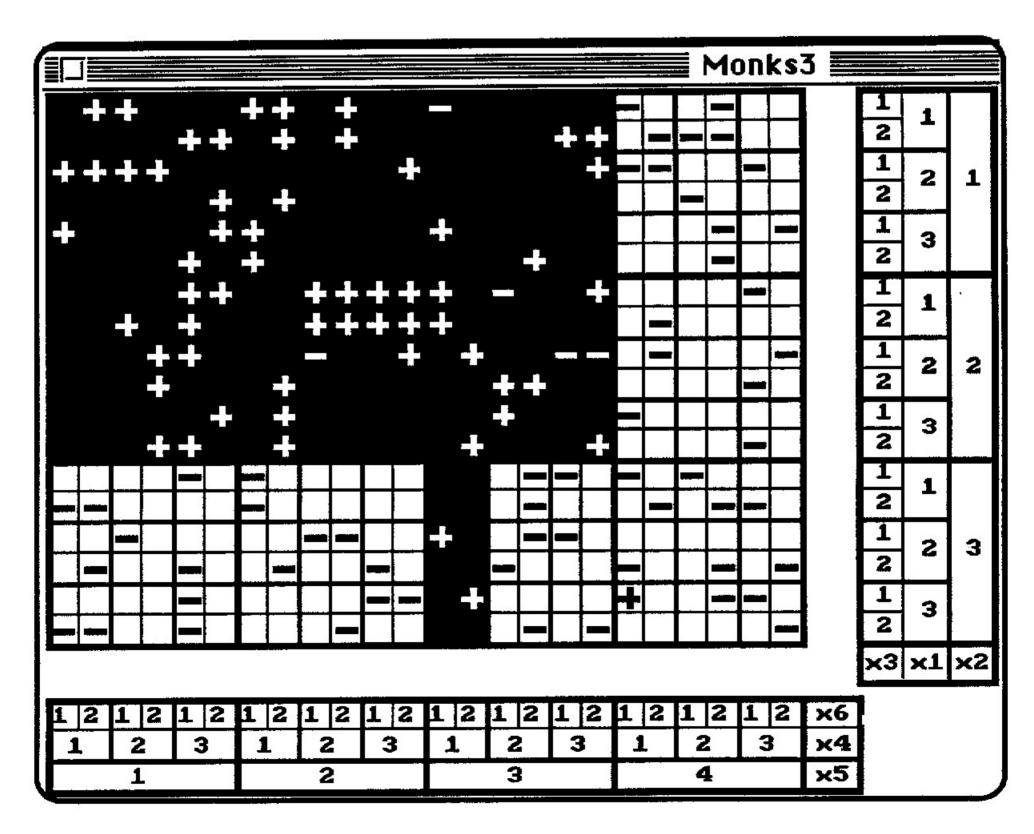


Figure 3. The third Monk's Problem

3.2. AQ17-DCI (Data-driven constructive induction)

This program is based on the classical AQ algorithm (Section 3.1), but it includes an algorithm for constructive induction that generates a number of new attributes. The quality of any generated attribute is evaluated according to a special Quality Function for attributes. If the Quality Function exceeds a certain threshold value, then the attribute is selected. A brief description of the algorithm for data-driven constructive induction (Bloedorn and Michalski, 1991) is given below. The program works in two phases.

Phase 1.

- 1. Identify all numeric-valued attributes.
- 2. Repeat steps 3 through 5 for each possible combination of these attributes, starting with the pairs of attributes, and extending them if their quality was found acceptable according to the attribute Quality Function (QF).
- 3. Repeat steps 4 and 5 for each constructive induction operator. The current operators include addition, subtraction, multiplication, integer division and logical comparison of attributes (Bloedorn and Michalski, 1991).
- 4. Calculate the values of the given attribute pair for the given constructive induction operator.
- 5. Evaluate the discriminatory power of this newly constructed attribute using the attribute Quality Function, described by Bloedorn and Michalski (1991). If the QF for an attribute is above an assumed threshold, then the attribute is stored, else it is discarded.
- 6. Repeat steps 4 and 5 for each available function operator that takes as argument an entire event (example), and calculate various global functions (properties) of it.

The program has a default list of global functions, but allows the user to modify the list to fit the problem at hand. The default list of functions include MAX (the maximum of the values of the numerical attributes in an event), MIN (the minimum value), AVE (the average value), MF (the most-frequent value), LF (least-frequent), and #VarEQ(x), which measures the number of variables (attributes) that take the value x in an example of a given class.

Phase 2.

- 1. Identify in the data all atributes that are binary.
- 2. Search for pairwise symmetry among the attributes and then for larger symmetry or approximate symmetry groups, based on the ideas described in (Michalski, 1969a; Jensen, 1975).
- 3. For each candidate symmetry group, create a new attribute that is the arithmetic sum of the attributes in the group.

- 4. Determine the quality function of the newly created attributes, and select the best attribute.
- 5. Enhance the dataset with values of this attribute, and induce new decision rules.

The method described above allows the system to express simply symmetric or partially symmetric Boolean functions and k-of-n functions, as well as more complex functions that depend on the presence of a certain number of attribute values in the data. Such functions are among the most difficult functions to express in terms of conventional logic operators.

3.3. AQ15-FCLS (Flexible concept learning)

This method (Zhang and Michalski, 1991) combines both symbolic and numeric representations in generating a concept description. The program is oriented toward learning flexible concepts, i.e, imprecise and context-dependent. To describe such concepts it creates two-tiered descriptions, which consist of a Basic Concept Representation (BCR) and an Inferential Concept Interpretation (ICI) to handle exceptions. In the program, the BCR is in the form of rules, and the ICI is in the form of a weighted evaluation function which sums up the contributions of individual conditions in a rule, and compares it with a THRESHOLD. The learning program learns both the rules and an appropriate value for the THRESHOLD.

Each rule of a concept description is learned in two steps, the first step is similar to the STAR algorithm in AQ that generates a general rule, and the second step optimizes the rule by specializing it and adjusting the accuracy threshold.

3.4. AQ17-HCI (Hypothesis-driven constructive induction)

AQ17-HCI (Hypothesis-Driven Constructive Induction) represents a module employed in the AQ17 attribute-based multistrategy constructive learning system. This module implements a new iterative constructive induction capability in which new attributes are generated based on the analysis of the hypotheses produced in the previous iteration (Wnek and Michalski, 1991). Input to the HCI module consists of the example set and a set of rules, in this case generated by the AQ15 program (Michalski et al, 1986). The rules are then evaluated according to a rule quality criterion, and the rules that score the best for each decision class are combined into new attributes. These attributes are incorporated into the set of training examples, and the learning process is repeated. The process continues until a termination criterion is satisfied. The method is a special implementation of the idea of the "survival of the fittest," and therefore can be viewed as a combination of symbolic learning with a form of genetic algorithm-based learning.

A brief description of the HCI algorithm follows:

- 1. Induce rules for each decision class using a standard AQ algorithm (as implemented in AQ15) from a subset of the available training examples.
- 2. Identify variables from the original set that are not present in the rules, and classify them as irrelevant.

- 3. For each decision class, generate a new attribute that represents the disjunction of of the highest quality rules.
- 4. Modify the training examples by adding the newly constructed attributes and removing the ones found to be irrelevant.
- 5. Induce rules from this modified training set.
- 6. Test these rules against the remainder of the training set. If the performance is not satisfactory, return to step 1. Otherwise, extend the initial complete set of training examples with the attributes from the obtained rules. Induce the final set of rules from this set of examples.

In these examples, the induction in steps 1, 5 and 6 used the learning algorithm implemented in the AQ15 program.

3.5. AQ14 - NT (noise-tolerant learning from engineering data)

The program implements an algorithm specially designed for learning from noisy engineering data (Pachowicz and Bala, 1991a and 1991b). The acquisition of concept descriptions (in the form of a set of decision rules) is performed in the following two phases:

• Phase 1:

Concept-driven closed-loop filtration of training data, where a single loop of gradual noise removal from the training dataset is composed of the following three stages:

1. Induce decision rules from a given dataset using the AQ14 (NEWGEM) inductive learning program.

2. Truncation of concept descriptions by removing "least significant" rules, that is, rules that cover only a small portion of the training data (this step is performed using the so-called TRUNC procedure).

3. Create a new training dataset that includes only training examples that are

covered by the truncated concept descriptions.

4. If the size of the dataset falls below an assumed percentage of the training data (that reflects an assumed error rate in the data), then go to Phase 2. Otherwise, return to step 1.

• Phase 2:

Acquire concept descriptions from the improved training dataset using the AQ14 learning program.

A justification for Phase 1 is that the noise in the data is unlikely to constitute any strong patterns in the data, and therefore will require separate rules to account for it. Thus, the examples covered by the "light rules" are likely to represent noise, and therefore are removed from the dataset. Experiments with AQ14-NT applied to a variety of engineering and computer vision problems have shown that it systematically produces classification rules that both perform better and also are much simpler.

3.6. AQ15-GA (AQ15 with attribute selection by a genetic algorithm)

In this approach (Vafaie and De Jong, 1991), genetic algorithms are used in conjunction with AQ15. Genetic algorithms are used to explore the space of all subsets of a given attribute set. Each of the selected attribute subsets is evaluated (its fitness measured) by invoking AQ15 and measuring the recognition rate of the rules produced.

The evaluation procedure as shown is divided into three main steps. After an attribute subset is selected, the initial training data, consisting of the entire set of attribute vectors and class assignments corresponding to examples from each of the given classes, is reduced. This is done by removing the values for attributes that were eliminated from the original attribute vector. The second step is to apply a classification process (AQ15) to the new reduced training data. The decision rules that AQ15 generates for each of the given classes in the training data are then used for classification. The last step is to use the rules produced by the AQ algorithm in order to evaluate the classification and hence, recognition with respect to the test data.

In order to use genetic algorithms as the search procedure, it is necessary to define a fitness function which properly assesses the decision rules generated by the AQ algorithm. The fitness function takes as an input a set of attribute or attribute definitions, a set of decision rules created by the AQ algorithm, and a collection of testing examples defining the attribute values for each example. The fitness function then views the AQ-generated rules as a form of class description that, when applied to a vector of attribute or attribute values, will evaluate to a number. It is evaluated for every attribute subset by applying the following steps: For every testing example a match score is evaluated for all the classification rules generated by the AQ algorithm, in order to find the rule(s) with the highest or best match. At the end of this process, if there is more than one rule having the highest match score, one rule will be selected based on the chosen conflict resolution process. This rule then represents the classification for the given testing example. If this is the appropriate classification, then the testing example has been recognized correctly. After all the testing examples have been classified, the overall fitness function will be evaluated by adding the weighted sum of the match score of all of the correct recognitions and subtracting the weighted sum of the match score of all of the incorrect recognitions.

4. RESULTS OF THE AQ PROGRAMS APPLIED TO THE MONKS' PROBLEMS

Below is a listing of the rules obtained by the various AQ programs (AQ17-DCI, AQ17-HCI, AQ15-GA, AQ15-FCLS or AQ14-NT), and the results of testing them on the testing examples. A listing of all the data, both training and testing sets, as provided by the creators of the problems, is in the Appendix.

Rules generated by different programs were tested using the ATEST program that computes a confusion matrix (Reinke, 1984). The program computes the so-called consonance degree between an unknown example and the rules for each decision class. The output from this program includes numerical evaluations of the the accuracy of the rules based on the percentage of the testing examples correctly classified (by choosing the rule that best fits the example), and the percentage of examples precisely matched by the correct decision rule. These percentages are output by ATEST as OVERALL % CORRECT-FLEX-MATCH and OVERALL % CORRECT-100% MATCH, respectively.

Details of the different programs, and of the AQ algorithm underlying these programs are given in Section 3. It should be noted that results are not always presented for each of these programs as applied to each of the three problems. As indicated above, these programs derive from the same basic method, each adding features appropriate to specific types of problems. The different programs derived basically the same rule for the first problem; the ones shown here are the ones whose knowledge representation schema allowed for the most elegant presentation of the output. We felt that for the sake of brevity and emphasis on the matching of the programs' different features with the types of problems to be solved, we should present only the results of the programs better suited for the given type of problem. For example, we felt that there was no reason to apply AQ14-NT, a program with special features to cope with noisy data to Problem 2, a problem in which data were without noise, and the testing events were 100% correctly classified by the rules obtained by other programs. For the same reason, we do not emphasize the results of the application of the data-driven constructive induction program AQ17-DCI to Problem 3; its algorithm is strictly data-driven, and as such is less suitable for learning from noisy data than other AO programs.

The results of applying the five AQ programs to the three Monks' problems are summarized in Table 2. The percentages represent the correct classification percentages as calculated by ATEST.

PROGRAM	#1	#2	#3
AQ17-DCI	100%	100%	97.2%
AQ17-HCI	100%	93.6%	100%
AQ15-FCLS	100%	92.6%	97.2%
AQ14-NT	100%	N/A	100%
AQ15-GA	100%	86.8%	100%

Table 2. Summary of AQ programs' correct classification percentages

4.1. Results for the 1st problem

4.1.1. Rules obtained by AQ17-DCI

These are the rules obtained by AQ17-DCI, a version of the AQ program that employs data-driven constructive induction. The results include 1 rule for Class 0 (that represents positive examples of the concept), and 2 rules for Class 1 (that represents the negative examples):

Class 0:

Rule 1 [jacket_color \neq red] & [head_shape <> body_shape] (total:62, unique:62)

Class 1:

Rule 1 [head_shape=body_shape] (total:41, unique:33)

Rule 2 [jacket_color=red] (total:29, unique:21)

In the above rules, expressions in [] denote individual conditions in a rule, "total" means the total number of training examples of the given class covered by the rule, and "unique" means the number of training examples covered by that rule only, and not by any other rules.

There is only one rule for Class 0, and there two rules for Class 1. The latter means that if either of the rules is matched by a given instance, then that instance is classified to Class 1. A set of such rules is logically equivalent to a disjuction of conjunctions. The syntax of the rules is defined formally according to the variable-valued logic calculus VL1. Individual rules corespond to "complexes" in VL1.

The results of applying the rules to the testing examples were:

RESULTS	991 N
OVERALL % CORRECT FLEX MATCH: OVERALL % CORRECT 100% MATCH:	

where:

% FLEX MATCH means the percentage of the correctly classified examples within the total set of testing examples, using a flexible matching function (see Reinke, 1984), and % 100% MATCH means that the percentage of correctly classified examples that matched the rules exactly.

The number of testing events satisfying individual rules in the correct class description is given in the table below:

		RULES		
		R1	R2	
CLASS	0	215		
CLASS	1	144	108	

4.1.2. Rules obtained by AQ17-HCI

These are the rules obtained by AQ17-HCI, a version of the AQ program that employs hypothesis-driven constructive induction (see section 3.4. The results include one rule for Class 0 that represents positive examples of the concept, and one rule for Class 1 that represents the negative examples:

Class 0:

Rule 1 [Neg=false] (total:62, unique:62)

Class 1:

Rule 1 [Pos=false] (total:62, unique:62)

where Neg and Pos are attributes constructed from the original ones, or intermediate ones, as defined below (these rules, as one can check, are logically equivalent to the AQ17-DCI generated rules)

```
c01 <:: [head_shape=round] & [body_shape≠round] & [jacket_color≠red] c05 <:: [head_shape=square] & [body_shape≠square] & [jacket_color≠red] c08 <:: [head_shape=octagon] & [body_shape≠octagon] & [jacket_color≠red] c10 <:: [head_shape=round] & [body_shape=round] c12 <:: [jacket_color=red] c13 <:: [head_shape=square] & [body_shape=square] c15 <:: [head_shape=octagon] & [body_shape=octagon] Pos <:: [c10=false] & [c12=false] & [c13=false] & [c15=false] Neg <:: [c01=false] & [c05=false] & [c08=false]
```

TEST RESULTS - SUMMARY	
OVERALL % CORRECT FLEX MATCH: OVERALL % CORRECT 100% MATCH:	

Number of testing events satisfying individual rules in the correct class description:

		RULES
CLASS	0	R 1 215
CLASS	1	216

Other programs either were either not used on this problem, or generated similar results.

4.2. Results for the 2nd problem

4.2.1. Rules obtained by AQ17-DCI

The rules below were obtained by AQ17-DCI, which is capable of generating all kinds of new attributes from the original attributes. For the problem at hand, the program found that a new attribute that expresses the number of variables in the learning examples that have some specific value is highly relevant to this problem. Such an attribute is assigned by the program the name #VarEQ(x), which means "the number of variables with value of rank k (in their domain)" in an example. The lowest value in the domain has rank 1, the next lowest has rank 2, etc. In this case, the relevant attribute was #VarEQ(1). Based on this attribute, the program constructed appropriate decision rules. There were two one-condition rules for Class 0, representing the positive examples of the concept, and one rule for Class 1 that represents the negative examples. The rule for Class 1 is logically equivalent to the negation of the union (disjunction) of the rules for Class 0.

Class 0:

Rule 1	[#VarEQ(1)>=3]
Rule 2	$[\text{#VarEQ}(1) \leq 1]$

Class 1:

Rule 1 [#VarEQ(1)=2]

The results of applying the rules to the testing examples were:

RESULTS	
OVERALL % CORRECT FLEX MATCH:	100.00
OVERALL % CORRECT 100% MATCH:	100.00

4.2.2. Rules obtained by AQ17-HCI

There are 4 top level rules for Class 0 (positive examples), and 6 top level rules for Class 1 (negative examples):

Class 0:

Rule 1	[Pos73=true] (total:90, unique:49)
Rule 2	[c14=false] & [c26=false] & [c53=false] & [c67=false] & [c72=false] &
	[Neg74=false] (total:38, unique:6)
Rule 3	[holding=2,3] & [c6=false] & [c20=false] & [Neg74=false]
	(total:22, unique:5)
Rule 4	[head_shape=2] & [has_tie=2] & [c44=false] & [c50=false] &
94369400 MINESTER 40	[Neg74=false] (total:6, unique:2)

Class 1:

Rule 1	[Neg74=true] (total:43, unique:30)
Rule 2	[jacket_color≠red] & [has_tie=true] & [c60=true] & [Pos73=false]
	(total: 17, unique: 4)
Rule 3	[head_shape≠round] & [body_shape=square] & [c28=false] &
	[Pos73=false] (total:16, unique:7)
Rule 4	body_shape=octagon] & [c48=true] & [c66=true] (total:4, unique:2)
Rule 5	[jacket_color=green] & [c43=true] & [c52=false] & [c53=false] &
	[c55=false] & [c69=true] & [Pos73=false] (total:4, unique:2)
Rule 6	[body_shape=octagon] & [c9=false] & [c10=true] & [c23=true] &
	[c32=true] (total:3, unique:1)

Attributes "ci, i=1..72" "Pos73," and "Neg74" were constructed during the learning process. The following were relevant to the discovered rules:

```
c2 <:: [jacket_color=red or blue]
c4 <:: [body_shape≠round] & [is_smiling=false]
c5 <:: [head_shape≠round] & [is_smiling=false]
c6 <:: [head_shape≠round] & [body_shape≠round]
```

```
c7 <:: [holding≠flag] & [jacket_color≠yellow]
c9 <:: [head_shape≠square] & [jacket_color≠red]
c10 <:: [holding≠flag] & [jacket_color≠red]
c14 <:: [jacket_color≠red] & [has_tie=false]
c15 <:: [is_smiling=true] & [jacket_color≠red]
c16 <:: [holding≠sword] & [has_tie=false]
c17 <:: [holding≠sword] & [jacket_color≠red]
c18 <:: [is_smiling=false] & [jacket_color≠red]
c20 <:: [jacket_color≠red] & [has_tie=true]
c21 <:: [body_shape≠round] & [holding≠sword]
c22 <:: [is_smiling=false] & [holding≠flag]
c23 <:: [holding=balloon] & [jacket_color=red]
c26 <:: [head_shape≠round] & [jacket_color≠red]
c28 <:: [body_shape≠square] & [jacket_color≠red]
c32 <:: [head_shape≠round] & [jacket_color≠blue]
c33 <:: [head_shape≠round] & [has_tie=false]
c37 <:: [is_smiling=false] & [holding≠sword]
c38 <:: [c21=false] & [c37=false]
c39 <:: [c6=true] & [c17=true]
c40 <:: [c5=true] & [c17=true]
c41 <:: [c15=false] & [c28=false]
c42 <:: [holding≠sword] & [c39=false]
c43 <:: [body_shape≠round] & [c39=false]
c44 <:: [holding=2,3] & [jacket_color≠red]
c46 <:: [c15=false] & [c39=false]
c47 <:: [c7=false] & [c39=false]
c48 <:: [jacket_color≠green] & [c7=false]
c49 <:: [c17=false] & [c33=true]
c50 <:: [body_shape≠round] & [c22=false]
c52 <:: [jacket_color\u00c4red] & [c14=false]
c53 <:: [jacket_color≠red] & [c21=true]
c55 <:: [holding≠flag] & [c14=false]
c56 <:: [holding \neq balloon] & [c14=false]
c59 <:: [jacket_color=yellow or blue]
c60 <:: [c38=false] & [c49=false]
c61 <:: [body_shape≠round] & [jacket_color≠red]
c65 <:: [c20=false] & [c39=false]
c66 <:: [jacket_color≠blue] & [c46=true]
c67 <:: [c38=false] & [c49=true]
c68 <:: [c40=false] & [c55=false]
c69 <:: [c16=false] & [c55=false]
c70 <:: [jacket_color=red] & [c18=false]
c72 <:: [jacket_color \neq blue] & [c37=true]
```

Pos73 <:: [c4=false] & [c16=false] & [c33=false] & [c39=false] & [c40=false] or [c15=false] & [c43=false] & [c47=false] & [c68=false] or [body_shape≠octagon] & [c21=false] & [c41=true] & [c44=false] & [c65=true] & [c67=false] or [c33=true] & [c60=true]

Neg74 <:: [c4=false] & [c42=true] & [c56=false] & [c65=true] & [c68=true] or [c2=false] & [c4=false] & [c16=false] & [c17=true] & [c26=true] or [is_smiling=false] & [holding≠sword] & [c14=false] & [c41=true] & [c43=true] &

TEST RESULTS - SUMMARY OVERALL % CORRECT FLEX MATCH: 93.06 OVERALL % CORRECT 100% MATCH: 86.57

The above summary of the results shows that the rules generated by AQ17-HCI approximate quite well the concept in Problem 2 although they use only logical operators. This result is quite interesting because concepts such as the one in Problem 2 are among the most difficult to learn using solely logic-based inductive learners (classical rule learning or decision tree learning programs). This result demonstrates the power of hypothesis-driven constructive induction.

Number of testing events satisfying individual complexes in the correct class description:

		RU	LES				
		R 1	R 2	R 3	R 4	R 5	R 6
CLASS	0	232	84	54	12		
CLASS	1	77	44	32	10	5	4

4.2.3. Rules obtained by AQ17-FCLS

These are the rules obtained by AQ17-FCLS, a version of the AQ program that learns flexible concepts by generating rules that permit partial matching. The threshold parameter indicates the minimum percentage of the individual conditions in the rule that must be satisfied for the rule to apply. The results include two rules for Class 0 that represent positive examples of the concept, and 18 rules for Class 1 that represent the negative examples. The discovered rules fully encompass Class 0, but they failed to get a complete grasp of the concept of Class 1:

Class 0:

Rule 1 [head_shape = round] & [body_shape = round] & [is_smiling = true] & [holding = sword] & [jacket_color = red] & [has_tie = true] with THRESHOLD = 50 %

(Total positive examples covered: 64)

This rule says that three or more variables must have rank equal to 1.

Rule 2 [head_shape \neq round] & [body_shape \neq round] & [is_smiling = false] & [holding \neq sword] & [jacket_color \neq red] & [has_tie = false] with THRESHOLD = 83 % (5/6)

(Total positive examples covered: 41)

This rule says that five or six out of six variables must not have their first values, or equivalently, that at most one variable may have its first value. Thus the disjunction of these two rules above indicates that the number of variables which have their first value cannot be equal to 2.

These rules classified correctly 100% of the examples of Class 0.

Class 1:

Since the current program does not have the ability to express the negation of the above two rules for Class 0, to program generated many "light-weight" rules to cover all examples of Class 1. The overall performance using the flexible match was not 100% beacuse in some cases when an example matched equally well the rules for both classes, an incorrect class was chosen. In the next version of the program, we will include the missing negation operator.

- Rule 1 [is_smiling = true] & [holding \neq sword] & [jacket_color = yellow] & [has_tie = false] with THRESHOLD = 100 % (Total positive examples covered: 8)
- Rule 2 [head_shape \neq round] & [body_shape \neq round] & [is_smiling = true] & [holding \neq sword] & [jacket_color \neq red] & [has_tie = true] with THRESHOLD = 100 % (Total positive examples covered: 9)
- Rule 3 [head_shape \neq round] & [body_shape \neq round] & [is_smiling = false] & [holding \neq sword] & [jacket_color = yellow] & [has_tie = false] with THRESHOLD = 100 % (Total positive examples covered: 7)
- Rule 4 [head_shape = octagon] & [body_shape = round] & [is_smiling = true] & [holding = sword] & [jacket_color = green] & [has_tie = false] with THRESHOLD = 83 % (Total positive examples covered: 5)
- Rule 5 [head_shape = round] & [is_smiling = true] & [holding ≠ sword] & [jacket_color = red or yellow] & [has_tie = false] with THRESHOLD = 100 % (Total positive examples covered: 5)
- Rule 6 [head_shape \neq round] & [body_shape = round] & [is_smiling = false] & [holding \neq flag] & [jacket_color = yellow] with THRESHOLD = 100 %

 (Total positive examples covered: 4)
- Rule 7 [head_shape = round] & [body_shape \neq round] & [is_smiling = false] & [holding \neq sword] & [jacket_color \neq red] & [has_tie = true] with THRESHOLD = 100 % (Total positive examples covered: 5)

- Rule 8 [head_shape ≠ round] & [is_smiling = false] & [jacket_color = red] & [has_tie = false] with THRESHOLD = 100 % (Total positive examples covered: 3)
- Rule 9 [head_shape \neq round] & [body_shape \neq round] & [is_smiling = false] & [holding = sword] & [jacket_color \neq red] & [has_tie = true] with THRESHOLD = 100 % (Total positive examples covered: 4)
- Rule 10 [head_shape ≠ square] & [body_shape = round] & [holding ≠ flag] & [jacket_color = blue] & [has_tie = false] with THRESHOLD = 100 % (Total positive examples covered: 3)
- Rule 11 [head_shape = square] & [body_shape = square] & [is_smiling = true] & [holding = sword] & [jacket_color ≠ red] & [has_tie = false] with THRESHOLD = 100 % (Total positive examples covered: 5)
- Rule 12 [head_shape ≠ octagon] & [body_shape = octagon] & [holding ≠ sword] & [jacket_color = red] & [has_tie = false] with THRESHOLD = 100 % (Total positive examples covered: 2)
- Rule 13 [head_shape = round] & [body_shape = round] & [is_smiling = false] & [holding = flag] & [jacket_color = yellow] & [has_tie = false] with THRESHOLD = 100 % (Total positive examples covered: 1)
- Rule 14 [head_shape = round] & [body_shape = octagon] & [is_smiling = false] & [holding = sword] & [jacket_color = red or green] & [has_tie = false] with THRESHOLD = 100 % (Total positive examples covered: 1)
- Rule 15 [head_shape = round] & [body_shape = square] & [is_smiling = false] & [holding \neq sword] & [jacket_color = red] & [has_tie = false] with THRESHOLD = 100 % (Total positive examples covered: 1)
- Rule 16 [head_shape = square] & [body_shape = round] & [is_smiling = true] & [holding = flag] & [jacket_color = yellow or green] with THRESHOLD = 100 % (Total positive examples covered: 2)
- Rule 17 [head_shape = octagon] & [body_shape = square] & [is_smiling = true] & [holding = balloon] & [jacket_color = red or yellow] with THRESHOLD = 100 % (Total positive examples covered: 2)
- Rule 18 [head_shape \neq round] & [body_shape = round] & [is_smiling = false] & [holding \neq sword] & [jacket_color \neq red] & [has_tie = true] with THRESHOLD = 100 %

(Total positive examples covered: 3)

TEST RESULTS - SUMMARY	
The percentage of correctly classified testing events: The percentage of correctly classified testing events in Class 0: The percentage of correctly classified testing events in Class 1: The total number of rules in the descriptions:	92.6% 100.0% 85.2% 2 for Class 0 18 for Class 1
The total number of conditions in the descriptions:	110

4.3. Results for the 3rd problem

4.3.1. Rules obtained by AQ17-HCI

Below are the rules obtained by the hypothesis-driven constructive induction method:

Class 0:

Rule 1 Rule 2	[Pos1=true] (total:49, unique:49) [body_shape≠round] & [holding≠sword] & [jacket_color=green] (total:11, unique:11)
Rule 3	[body_shape=round] & [holding=sword] & [jacket_color=green] (total:1, unique:1)
Rule 4	[body_shape=square] & [holding=balloon] & [jacket_color=yellow] (total:1, unique:1)

Class 1:

Kule 1	[Neg2=true] (total:5/, unique:5/)
Rule 2	body_shape=octagon] & [holding=sword] & [jacket_color=green or blue]
	(total:3, unique:3)

where Pos1 and Neg2 are attributes constructed from the original ones (Wnek & Michalski, 1991)

Pos1 <:: [jacket_color=blue] or [body_shape=octagon] & [jacket_color≠green]

Neg2 <:: [body_shape≠octagon] & [jacket_color≠blue]

TEST RESULTS - SUMMARY	
OVERALL % CORRECT FLEX MATCH:	100.00
OVERALL % CORRECT 100% MATCH:	86.11

Since this problem involves noisy data, the flexible match should always be used. The results from 100% match are shown just for comparison.

Number of testing events satisfying individual rules in the correct class description:

		RULES			
		R 1	R 2	R 3	R 4
CLASS	0	180	24	0	0
CLASS	1	216	12		

4.3.2. Rules obtained by AQ14-NT

These are the rules obtained by AQ14-NT, a version of the AQ program that employs a noise-filtration technique. The results include one rule for Class 0 that represents positive examples of the concept, and one rule for Class 1 that represents negative examples.

After only two loops of concept-driven filtration of training dataset (with truncation parameter equal to 10%) and repeated learning, we received the following set of rules:

Class 0:

Rule 1 Rule 2 Rule 3	[jacket_color=blue] [body_shape=octagon] & [holding≠sword] [body_shape=octagon] & [jacket_color=red or yellow]
Class 1:	
Rule 1 Rule 2	[body_shape=octagon] & [jacket_color=blue] [holding=sword] & [jacket_color=green]

These rules recognized all test data correctly, i.e., on the 100% level.

Since there was supposed to be noise in the data, we are somewhat surprised by such a high degree of recognition.

4.3.3. Rules obtained by AQ17-FCLS

These are the rules obtained by AQ17-FCLS. The results include two rules for Class 0 that represent positive examples of the concept, and one rule for Class 1 that represents the negative examples. The threshold parameter indicates the minimum percentage of selectors in the rule that must be true for the rule to apply. This set of rules is intentionally incomplete and inconsistent with the training set since it was generated with a 10% error tolerance. This produced better results than other tolerances that were tried.

Class 0:

Rule 1 [head_shape \neq round] & [body_shape = octagon] & [jacket_color = blue] with THRESHOLD = 67 %

(Total positive examples covered: 42)

Rule 2 [head_shape = round] & [body_shape = octagon] & [jacket_color = blue] with THRESHOLD = 67 %

(Total positive examples covered: 26)

Class 1:

Rule 1 [body_shape = red or yellow] & [jacket_color ≠ blue] with THRESHOLD = 100 % (Total positive examples covered: 57)

TEST RESULTS - SUMMARY	
The percentage of correctly classified testing events: The percentage of correctly classified testing events in Class 0: The percentage of correctly classified testing events in Class 1: The total number of rules in the descriptions:	97.2% 100.0% 94.7% 2 for Class 0 1 for Class 1
The total number of conditions in the descriptions:	8

4.3.4. Rules obtained by AQ15-GA

Below are the rules obtained by AQ15-GA, a program that uses a genetic algorithm in conjunction with the AQ rule-generation algorithm. The first rule is for the positive examples of the concept, Class 0, and the second for the negative examples, Class 1. A genetic algorithm determined that 3 attributes (body_shape, holding, and jacket_color) were the most meaningful. Using these, the rules discovered were as follows:

Class 0:

Rule I	[jacket_color=blue]
Rule 2	[body_shape=octagon] & [jacket_color=red or yellow]
Rule 3	[body_shape≠round] & [holding≠sword] & [jacket_color=green]
Rule 4	[body_shape=round] & [holding=sword] & [jacket_color=green]
Rule 5	[body_shape=square] & [holding=2] & [jacket_color=yellow]

Class 1:

Rule 1	[body_shape≠octagon] & [jacket_color≠blue]
Rule 2	[body_shape=octagon] & [holding=sword] & [jacket_color=green or blue]

Results on testing the rules on testing events using program ATEST:

TEST RESULTS - SUMMARY	
OVERALL % CORRECT FLEX MATCH	사용되어 - 11는 14일 구경하고 12일 구성하고 1

5. COMPARISON OF AQ WITH OTHER PROGRAMS

In the Thrun study (Thrun et al, 1991), the AQ programs performed very favorably in comparison with the other programs examined (Table 3). Programs and algorithms that were tested on these problems included Assistant Professional (Cestnik, Kononenko and Bratko); mFOIL (Dzeroski); ID5R, IDL, ID5R-hat and TDIDT (Van de Velde); ID3 (with and without windowing), ID5R, AQR, CN2 and CLASSWEB (Kreuziger, Hamman and Wenzel); PRISM (Keller); ECOBWEB (Reich and Fisher); Backpropagation (Thrun) and Cascade Correlation (Fahlman).

PROGRAM	#1	#2	#3
AQ17-DCI AQ17-HCI AQ15-FCLS	100% 100%	100% 93.1% 92.6%	94.2% 100% 97.2% 100%
AQ14-NT AQ15-GA	100%	86.8%	100%
Assistant Professional	100%	81.3%	100%
mFOIL	100%	69.2%	100%
ID5R IDL ID5R-hat TDIDT	81.7% 97.2% 90.3% 75.7 %	61.8% 66.2% 65.7% 66.7%	
ID3 ID3, no windowing ID5R AQR CN2 CLASSWEB 0.10 CLASSWEB 0.15 CLASSWEB 0.20	98.6% 83.2% 79.7% 95.9% 100% 71.8% 65.7% 63.0%	67.9% 69.1% 69.2% 79.7% 69.0% 64.8% 61.6% 57.2%	94.4% 95.6% 95.2% 87.0% 89.1% 80.8% 85.4% 75.2%
PRISM	86.3%	72.7%	90.3%
ECOBWEB leaf prediction ECOBWEB l.p. & information utility	71.8% 82.7%	67.4% 71.3%	68.2% 68.0%
Backpropagation Backprop. with weight decay	100% 100%	100% 100%	93.1% 97.2%
Cascade Correlation	100%	100%	97.2%

Table 3. Summary of classification results reported by Thrun

These results include an earlier result from AQ17-DCI for problem 3 that has since been improved upon. While the results do not guarantee either that all the programs were employed with optimal parameter settings or that these results can be extended to other concept learning problems, it is interesting to note that only the rule-based AQ programs were able to come up with 100% classification rates on both the k-of-n concept and the noisy concept. In addition, the lower bounds on the classification rates of the AQ programs were very respectable in comparison with the other programs, indicating that these programs can generate reasonable results, even when the optimal tool is not being used.

An earlier study by Wnek, Sarma, Wahab and Michalski (1990) compared the standard version of AQ15, a backpropagation neural net, the CFS classifier system and the C4.5 decision tree learning program by testing their ability to learn five concepts created by human subjects. Their results indicated that the symbolic algorithms were better suited toward these symbolic-oriented problems, both in terms of error rate and knowledge complexity.

Spears and Gordon (1991) compared NEWGEM (a predecessor to AQ15), C4.5, and GABIL, a genetic algorithm-based system, on an artificial disjuncts-and-conjuncts domain and on breast cancer case data. They found comparable error rates among the systems and proposed a multistrategy system that would improve the GABIL results by incorporating elements of other systems in the form of genetic operators.

Bergadano, Matwin, Michalski and Zhang (1990) compared three AQ-based systems with ASSISTANT and with an exemplar-based method on two real world domains, congressional voting and labor negotiations. The AQ programs generated simpler and more accurate rules, particularly when flexible concept learning (such as in AQ15-FCLS) was employed.

6. CONCLUSION

When tested on the Monks' problems, the AQ-based programs were able to generate rules that closely approximated or exactly matched the target concepts. By choosing the proper program, users could generate a simple and accurate concept representation.

Researchers have been turning more frequently to comparisons of different learning paradigms. No single set of test problems will generate results that will hold true universally. Nonetheless, by performing different comparisons, and by establishing diverse sets of benchmark problems, we can begin to discover details of the suitability of different learning methods to different types of problems.

By combining some of the specialized techniques and modules, a more powerful and versatile module can be created. For example, an ongoing project involves the integration of the DCI and HCI modules of AQ17 into a single unit. An important topic of this research (and of many other multistrategy projects) is the development of a unified control system that can integrate smoothly the capabilities of the different techniques.

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APPENDIX: INPUT DATA FOR THE THREE MONKS' PROBLEMS

Below are the training and testing data sets that were presented to us for the Monks' Problems. In each of the problems, the testing set consisted of the entire event space, and as such was a superset of the training set. This has an effect on some of the numeric results of the ATEST analyses of the rules discovered by the various programs.

The examples are presented in the following format:

```
Ex. #: x1 x2 x3 x4 x5 x6 -> C
```

where # is the position of the example in the lexicographic ordering of the event space, xi represents the value of the ith variable, and C is the class to which the example is assigned.

Training Data Set #1

The training set of examples for the first problem:
(head_shape = body_shape) or (jacket color = red)

```
Ex. 210: 221312 -> 1
Ex. 5: 111131 -> 1
                        Ex. 119: 131341 -> 0
                                                 Ex. 212: 221322 -> 1
Ex. 6: 111132 -> 1
                        Ex. 120: 131342 -> 0
                        Ex. 124: 132122 -> 0
                                                 Ex. 214: 221332 -> 1
Ex. 19: 111321 -> 1
                                                 Ex. 216: 221342 -> 1
                        Ex. 130: 132212 -> 1
Ex. 22: 111332 -> 1
                                                 Ex. 217: 222111 -> 1
                        Ex. 132: 132222 -> 0
Ex. 27: 1 1 2 1 2 1 -> 1
                        Ex. 134: 132232 -> 0
                                                 Ex. 222: 222132 -> 1
Ex. 28: 112122 -> 1
                                                 Ex. 223: 2 2 2 1 4 1 -> 1
                        Ex. 135: 132241 -> 0
Ex. 37: 112231 -> 1
                                                 Ex. 224: 222142 -> 1
Ex. 39: 112241 -> 1
                        Ex. 136: 132242 -> 0
                                                 Ex. 227: 22221 -> 1
Ex. 42: 112312 -> 1
                        Ex. 137: 132311 -> 1
                                                 Ex. 239: 222341 -> 1
                        Ex. 139: 132321 -> 0
Ex. 50: 121112 -> 1
                        Ex. 143: 132341 -> 0
                                                 Ex. 241: 231111 -> 1
Ex. 51: 121121 -> 0
                                                 Ex. 249: 231211 -> 1
Ex. 53: 121131 -> 0
                        Ex. 144: 132342 -> 0
                                                 Ex. 253: 231231 -> 0
Ex. 56: 121142 -> 0
                        Ex. 149: 211131 -> 0
                                                 Ex. 258: 231312 -> 1
                        Ex. 150: 211132 -> 0
Ex. 57: 121211 -> 1
                                                 Ex. 261: 231331 -> 0
                        Ex. 153: 211211 -> 1
Ex. 61: 121231 -> 0
                                                 Ex. 264: 231342 -> 0
                        Ex. 154: 211212 -> 1
Ex. 62: 121232 -> 0
                        Ex. 156: 211222 -> 0
                                                 Ex. 270: 232132 -> 0
Ex. 64: 121242 -> 0
                        Ex. 157: 211231 -> 0
                                                 Ex. 273: 232211 -> 1
Ex. 67: 121321 -> 0
                                                 Ex. 274: 232212 -> 1
Ex. 72: 121342 -> 0
                        Ex. 159: 211241 -> 0
                        Ex. 160: 211242 -> 0
                                                 Ex. 275: 232221 -> 0
Ex. 76: 122122 -> 0
                                                 Ex. 286: 232332 -> 0
                        Ex. 167: 211341 -> 0
Ex. 86: 122232 -> 0
                                                 Ex. 289: 3 1 1 1 1 1 -> 1
Ex. 87: 122241 -> 0
                        Ex. 172: 212122 -> 0
                        Ex. 173: 2 1 2 1 3 1 -> 0
                                                 Ex. 290: 3 1 1 1 1 2 -> 1
Ex. 88: 122242 -> 0
                                                 Ex. 297: 3 1 1 2 1 1 -> 1
Ex. 92: 122322 -> 0
                        Ex. 176: 212142 -> 0
                                                 Ex. 300: 311222 -> 0
                        Ex. 181: 212231 -> 0
Ex. 93: 122331 -> 0
                                                 Ex. 308: 3 1 1 3 2 2 -> 0
                        Ex. 184: 212242 -> 0
Ex. 94: 122332 -> 0
                                                 Ex. 313: 3 1 2 1 1 1 -> 1
                        Ex. 188: 212322 -> 0
Ex. 99: 131121 -> 0
                                                 Ex. 316: 312122 -> 0
                        Ex. 191: 212341 -> 0
Ex. 103: 131141 -> 0
                                                 Ex. 324: 312222 -> 0
                        Ex. 195: 221121 -> 1
Ex. 107: 131221 -> 0
                        Ex. 196: 221122 -> 1
                                                 Ex. 326: 312232 -> 0
Ex. 111: 131241 -> 0
                        Ex. 197: 221131 -> 1
                                                 Ex. 332: 312322 -> 0
Ex. 114: 131312 -> 1
                        Ex. 206: 221232 -> 1
                                                 Ex. 337: 3 2 1 1 1 1 -> 1
Ex. 116: 131322 -> 0
                                                 Ex. 344: 3 2 1 1 4 2 -> 0
                        Ex. 209: 221311 -> 1
Ex. 117: 131331 -> 0
```

Ex. 346: 3 2 1 2 1 2 -> 1	Ex. 387: 3 3 1 1 2 1 -> 1	Ex. 414: 332132 -> 1
Ex. 352: 3 2 1 2 4 2 -> 0	Ex. 392: 3 3 1 1 4 2 -> 1	Ex. 415: 332141 -> 1
Ex. 361: 3 2 2 1 1 1 -> 1	Ex. 398: 3 3 1 2 3 2 -> 1	Ex. 416: 332142 -> 1
Ex. 362: 3 2 2 1 1 2 -> 1	Ex. 400: 331242 -> 1	Ex. 426: 3 3 2 3 1 2 -> 1
Ex. 366: 3 2 2 1 3 2 -> 0	Ex. 402: 331312 -> 1	Ex. 428: 332322 -> 1
Ex. 377: 3 2 2 3 1 1 -> 1	Ex. 403: 3 3 1 3 2 1 -> 1	Ex. 430: 332332 -> 1
Ex. 379: 3 2 2 3 2 1 -> 0	Ex. 404: 3 3 1 3 2 2 -> 1	Ex. 432: 3 3 2 3 4 2 -> 1
Ex. 383: 3 2 2 3 4 1 -> 0	Ex. 408: 3 3 1 3 4 2 -> 1	
Ex. 385: 3 3 1 1 1 1 -> 1	Ex. 409: 3 3 2 1 1 1 -> 1	

Testing Data Set #1

```
Ex. 83: 122221 -> 0
                        Ex. 42: 112312 -> 1
Ex. 1: 111111 -> 1
                                                 Ex. 84: 122222 -> 0
                        Ex. 43: 112321 -> 1
Ex. 2: 111112 -> 1
                        Ex. 44: 112322 -> 1
                                                 Ex. 85: 122231 -> 0
Ex. 3: 111121 -> 1
                                                 Ex. 86: 122232 -> 0
                        Ex. 45: 112331 -> 1
Ex. 4: 111122 -> 1
                                                 Ex. 87: 122241 -> 0
Ex. 5: 111131 -> 1
                        Ex. 46: 112332 -> 1
                                                 Ex. 88: 122242 -> 0
                        Ex. 47: 112341 -> 1
Ex. 6: 111132 -> 1
                                                 Ex. 89: 122311 -> 1
                        Ex. 48: 112342 -> 1
Ex. 7: 111141 -> 1
                                                Ex. 90: 122312 -> 1
                        Ex. 49: 121111 -> 1
Ex. 8: 111142 -> 1
                                                 Ex. 91: 122321 -> 0
                        Ex. 50: 121112 -> 1
Ex. 9: 111211 -> 1
                                                Ex. 92: 122322 -> 0
                        Ex. 51: 121121 -> 0
Ex. 10: 111212 -> 1
                                                 Ex. 93: 122331 -> 0
                        Ex. 52: 121122 -> 0
Ex. 11: 111221 -> 1
                        Ex. 53: 121131 -> 0
                                                 Ex. 94: 122332 -> 0
Ex. 12: 1 1 1 2 2 2 -> 1
                                                 Ex. 95: 122341 -> 0
Ex. 13: 1 1 1 2 3 1 -> 1
                        Ex. 54: 121132 -> 0
                                                 Ex. 96: 122342 -> 0
                        Ex. 55: 121141 -> 0
Ex. 14: 111232 -> 1
                        Ex. 56: 121142 -> 0
Ex. 15: 111241 -> 1
                                                 Ex. 97: 131111 -> 1
                        Ex. 57: 121211 -> 1
                                                 Ex. 98: 131112 -> 1
Ex. 16: 111242 -> 1
                                                 Ex. 99: 131121 -> 0
Ex. 17: 111311 -> 1
                        Ex. 58: 121212 -> 1
Ex. 18: 1 1 1 3 1 2 -> 1
                        Ex. 59: 121221 -> 0
                                                 Ex. 100: 131122 -> 0
Ex. 19: 111321 -> 1
                        Ex. 60: 121222 -> 0
                                                 Ex. 101: 131131 -> 0
                        Ex. 61: 121231 -> 0
Ex. 20: 1 1 1 3 2 2 -> 1
                                                 Ex. 102: 131132 -> 0
Ex. 21: 111331 -> 1
                        Ex. 62: 121232 -> 0
                                                 Ex. 103: 131141 -> 0
                        Ex. 63: 121241 -> 0
                                                Ex. 104: 131142 -> 0
Ex. 22: 111332 -> 1
                                                Ex. 105: 131211 -> 1
                        Ex. 64: 121242 -> 0
Ex. 23: 111341 -> 1
Ex. 24: 111342 -> 1
                                                Ex. 106: 131212 -> 1
                        Ex. 65: 121311 -> 1
                        Ex. 66: 121312 -> 1
                                                Ex. 107: 131221 -> 0
Ex. 25: 112111 -> 1
Ex. 26: 112112 -> 1
                        Ex. 67: 121321 -> 0
                                                Ex. 108: 131222 -> 0
                                                 Ex. 109: 131231 -> 0
                        Ex. 68: 121322 -> 0
Ex. 27: 112121 -> 1
Ex. 28: 112122 -> 1
                        Ex. 69: 121331 -> 0
                                                Ex. 110: 131232 -> 0
                                                Ex. 111: 131241 -> 0
Ex. 29: 112131 -> 1
                        Ex. 70: 121332 -> 0
                        Ex. 71: 121341 -> 0
Ex. 30: 112132 -> 1
                                                Ex. 112: 131242 -> 0
                        Ex. 72: 121342 -> 0
                                                Ex. 113: 131311 -> 1
Ex. 31: 112141 -> 1
Ex. 32: 112142 -> 1
                        Ex. 73: 122111 -> 1
                                                Ex. 114: 131312 -> 1
                        Ex. 74: 122112 -> 1
Ex. 33: 112211 -> 1
                                                Ex. 115: 131321 -> 0
                        Ex. 75: 122121 -> 0
Ex. 34: 112212 -> 1
                                                Ex. 116: 131322 -> 0
Ex. 35: 112221 -> 1
                        Ex. 76: 122122 -> 0
                                                Ex. 117: 131331 -> 0
                        Ex. 77: 122131 -> 0
Ex. 36: 112222 -> 1
                                                Ex. 118: 131332 -> 0
                        Ex. 78: 122132 -> 0
                                                Ex. 119: 131341 -> 0
Ex. 37: 112231 -> 1
Ex. 38: 112232 -> 1
                        Ex. 79: 122141 -> 0
                                                Ex. 120: 131342 -> 0
                        Ex. 80: 122142 -> 0
                                                Ex. 121: 132111 -> 1
Ex. 39: 112241 -> 1
Ex. 40: 112242 -> 1
                        Ex. 81: 122211 -> 1
                                                Ex. 122: 132112 -> 1
                                                Ex. 123: 132121 -> 0
                        Ex. 82: 122212 -> 1
Ex. 41: 112311 -> 1
```

```
Ex. 232: 222242 -> 1
                        Ex. 178: 212212 -> 1
Ex. 124: 132122 -> 0
                                                Ex. 233: 222311 -> 1
                        Ex. 179: 212221 -> 0
Ex. 125: 132131 -> 0
                        Ex. 180: 212222 -> 0
                                                Ex. 234: 222312 -> 1
Ex. 126: 132132 -> 0
                                                Ex. 235: 222321 -> 1
                        Ex. 181: 212231 -> 0
Ex. 127: 132141 -> 0
                                                 Ex. 236: 222322 -> 1
                        Ex. 182: 212232 -> 0
Ex. 128: 132142 -> 0
                                                 Ex. 237: 222331 -> 1
                        Ex. 183: 212241 -> 0
Ex. 129: 132211 -> 1
                        Ex. 184: 212242 -> 0
                                                Ex. 238: 222332 -> 1
Ex. 130: 132212 -> 1
                                                Ex. 239: 222341 -> 1
                        Ex. 185: 212311 -> 1
Ex. 131: 132221 -> 0
                                                Ex. 240: 222342 -> 1
                        Ex. 186: 212312 -> 1
Ex. 132: 132222 -> 0
                                                Ex. 241: 231111 -> 1
Ex. 133: 132231 -> 0
                        Ex. 187: 212321 -> 0
                        Ex. 188: 212322 -> 0
                                                Ex. 242: 231112 -> 1
Ex. 134: 132232 -> 0
                        Ex. 189: 212331 -> 0
                                                Ex. 243: 231121 -> 0
Ex. 135: 132241 -> 0
                                                Ex. 244: 231122 -> 0
                        Ex. 190: 212332 -> 0
Ex. 136: 132242 -> 0
                                                Ex. 245: 231131 -> 0
                        Ex. 191: 212341 -> 0
Ex. 137: 132311 -> 1
                                                Ex. 246: 231132 -> 0
                        Ex. 192: 212342 -> 0
Ex. 138: 132312 -> 1
                                                Ex. 247: 231141 -> 0
                        Ex. 193: 221111 -> 1
Ex. 139: 132321 -> 0
Ex. 140: 132322 -> 0
                        Ex. 194: 221112 -> 1
                                                Ex. 248: 231142 -> 0
                                                Ex. 249: 231211 -> 1
                        Ex. 195: 221121 -> 1
Ex. 141: 132331 -> 0
                                                Ex. 250: 231212 -> 1
                        Ex. 196: 221122 -> 1
Ex. 142: 132332 -> 0
                                                Ex. 251: 231221 -> 0
                        Ex. 197: 221131 -> 1
Ex. 143: 132341 -> 0
                                                Ex. 252: 231222 -> 0
                        Ex. 198: 221132 -> 1
Ex. 144: 132342 -> 0
                        Ex. 199: 221141 -> 1
                                                Ex. 253: 231231 -> 0
Ex. 145: 2 1 1 1 1 1 -> 1
                        Ex. 200: 221142 -> 1
                                                Ex. 254: 231232 -> 0
Ex. 146: 211112 -> 1
                                                Ex. 255: 231241 -> 0
Ex. 147: 211121 -> 0
                        Ex. 201: 2 2 1 2 1 1 -> 1
                                                Ex. 256: 231242 -> 0
                        Ex. 202: 221212 -> 1
Ex. 148: 211122 -> 0
                                                Ex. 257: 231311 -> 1
                        Ex. 203: 221221 -> 1
Ex. 149: 211131 -> 0
                        Ex. 204: 221222 -> 1
                                                Ex. 258: 231312 -> 1
Ex. 150: 211132 -> 0
                        Ex. 205: 221231 -> 1
                                                Ex. 259: 231321 -> 0
Ex. 151: 2 1 1 1 4 1 -> 0
                                                Ex. 260: 231322 -> 0
                        Ex. 206: 221232 -> 1
Ex. 152: 211142 -> 0
                        Ex. 207: 221241 -> 1
                                                Ex. 261: 231331 -> 0
Ex. 153: 211211 -> 1
                                                Ex. 262: 231332 -> 0
Ex. 154: 211212 -> 1
                        Ex. 208: 221242 -> 1
                        Ex. 209: 221311 -> 1
                                                Ex. 263: 231341 -> 0
Ex. 155: 211221 -> 0
                                                Ex. 264: 231342 -> 0
Ex. 156: 211222 -> 0
                        Ex. 210: 221312 -> 1
                                                Ex. 265: 232111 -> 1
                        Ex. 211: 221321 -> 1
Ex. 157: 211231 -> 0
Ex. 158: 211232 -> 0
                        Ex. 212: 221322 -> 1
                                                Ex. 266: 232112 -> 1
                                                Ex. 267: 232121 -> 0
                        Ex. 213: 221331 -> 1
Ex. 159: 211241 -> 0
                                                Ex. 268: 232122 -> 0
                        Ex. 214: 221332 -> 1
Ex. 160: 211242 -> 0
                        Ex. 215: 221341 -> 1
                                                Ex. 269: 232131 -> 0
Ex. 161: 211311 -> 1
                                                Ex. 270: 232132 -> 0
Ex. 162: 211312 -> 1
                        Ex. 216: 221342 -> 1
                        Ex. 217: 222111 -> 1
                                                Ex. 271: 232141 -> 0
Ex. 163: 211321 -> 0
Ex. 164: 211322 -> 0
                        Ex. 218: 222112 -> 1
                                                Ex. 272: 232142 -> 0
                        Ex. 219: 222121 -> 1
                                                Ex. 273: 232211 -> 1
Ex. 165: 211331 -> 0
                                                Ex. 274: 232212 -> 1
                        Ex. 220: 222122 -> 1
Ex. 166: 211332 -> 0
                        Ex. 221: 222131 -> 1
                                                Ex. 275: 232221 -> 0
Ex. 167: 211341 -> 0
                        Ex. 222: 222132 -> 1
                                                Ex. 276: 232222 -> 0
Ex. 168: 211342 -> 0
                                                Ex. 277: 232231 -> 0
                        Ex. 223: 222141 -> 1
Ex. 169: 212111 -> 1
                                                Ex. 278: 232232 -> 0
                        Ex. 224: 222142 -> 1
Ex. 170: 212112 -> 1
                                                Ex. 279: 232241 -> 0
Ex. 171: 212121 -> 0
                        Ex. 225: 2 2 2 2 1 1 -> 1
                        Ex. 226: 222212 -> 1
                                                Ex. 280: 232242 -> 0
Ex. 172: 2 1 2 1 2 2 -> 0
                                                Ex. 281: 232311 -> 1
                        Ex. 227: 22221 -> 1
Ex. 173: 2 1 2 1 3 1 -> 0
                                                Ex. 282: 232312 -> 1
                        Ex. 228: 22222 -> 1
Ex. 174: 212132 -> 0
                                                Ex. 283: 232321 -> 0
                        Ex. 229: 22231 -> 1
Ex. 175: 212141 -> 0
                                                Ex. 284: 232322 -> 0
                        Ex. 230: 222232 -> 1
Ex. 176: 212142 -> 0
                        Ex. 231: 222241 -> 1
                                                Ex. 285: 232331 -> 0
Ex. 177: 212211 -> 1
```

```
Ex. 335: 312341 -> 0
                                                      Ex. 384: 322342 -> 0
Ex. 286: 232332 -> 0
                           Ex. 336: 312342 -> 0
                                                      Ex. 385: 3 3 1 1 1 1 -> 1
Ex. 287: 232341 -> 0
                                                      Ex. 386: 3 3 1 1 1 2 -> 1
                           Ex. 337: 3 2 1 1 1 1 -> 1
Ex. 288: 232342 -> 0
                                                      Ex. 387: 3 3 1 1 2 1 -> 1
                           Ex. 338: 3 2 1 1 1 2 -> 1
Ex. 289: 3 1 1 1 1 1 -> 1
                                                      Ex. 388: 3 3 1 1 2 2 -> 1
                           Ex. 339: 3 2 1 1 2 1 -> 0
Ex. 290: 311112 -> 1
                                                      Ex. 389: 3 3 1 1 3 1 -> 1
                           Ex. 340: 3 2 1 1 2 2 -> 0
Ex. 291: 3 1 1 1 2 1 -> 0
                                                      Ex. 390: 3 3 1 1 3 2 -> 1
                           Ex. 341: 3 2 1 1 3 1 -> 0
Ex. 292: 3 1 1 1 2 2 -> 0
                                                      Ex. 391: 3 3 1 1 4 1 -> 1
                           Ex. 342: 3 2 1 1 3 2 -> 0
Ex. 293: 3 1 1 1 3 1 -> 0
                                                      Ex. 392: 3 3 1 1 4 2 -> 1
                           Ex. 343: 3 2 1 1 4 1 -> 0
Ex. 294: 311132 -> 0
                                                      Ex. 393: 3 3 1 2 1 1 -> 1
                           Ex. 344: 3 2 1 1 4 2 -> 0
Ex. 295: 311141 -> 0
                                                      Ex. 394: 331212 -> 1
                           Ex. 345: 3 2 1 2 1 1 -> 1
Ex. 296: 311142 -> 0
                           Ex. 346: 3 2 1 2 1 2 -> 1
                                                      Ex. 395: 331221 -> 1
Ex. 297: 3 1 1 2 1 1 -> 1
                                                      Ex. 396: 331222 -> 1
                           Ex. 347: 3 2 1 2 2 1 -> 0
Ex. 298: 311212 -> 1
                                                      Ex. 397: 3 3 1 2 3 1 -> 1
                           Ex. 348: 321222 -> 0
Ex. 299: 311221 -> 0
                           Ex. 349: 3 2 1 2 3 1 -> 0
                                                      Ex. 398: 331232 -> 1
Ex. 300: 3 1 1 2 2 2 -> 0
Ex. 301: 3 1 1 2 3 1 -> 0
                                                      Ex. 399: 331241 -> 1
                           Ex. 350: 3 2 1 2 3 2 -> 0
                                                      Ex. 400: 331242 -> 1
                           Ex. 351: 3 2 1 2 4 1 -> 0
Ex. 302: 3 1 1 2 3 2 -> 0
                                                      Ex. 401: 331311 -> 1
Ex. 303: 3 1 1 2 4 1 -> 0
                           Ex. 352: 3 2 1 2 4 2 -> 0
                                                      Ex. 402: 331312 -> 1
                           Ex. 353: 3 2 1 3 1 1 -> 1
Ex. 304: 3 1 1 2 4 2 -> 0
                           Ex. 354: 321312 -> 1
                                                      Ex. 403: 331321 -> 1
Ex. 305: 311311 -> 1
                                                      Ex. 404: 331322 -> 1
                           Ex. 355: 321321 -> 0
Ex. 306: 311312 -> 1
                                                      Ex. 405: 331331 -> 1
                           Ex. 356: 321322 -> 0
Ex. 307: 3 1 1 3 2 1 -> 0
                                                      Ex. 406: 331332 -> 1
                           Ex. 357: 3 2 1 3 3 1 -> 0
Ex. 308: 311322 -> 0
                                                      Ex. 407: 3 3 1 3 4 1 -> 1
                           Ex. 358: 3 2 1 3 3 2 -> 0
Ex. 309: 3 1 1 3 3 1 -> 0
Ex. 310: 3 1 1 3 3 2 -> 0
                           Ex. 359: 321341 -> 0
                                                      Ex. 408: 331342 -> 1
                                                      Ex. 409: 332111 -> 1
                           Ex. 360: 321342 -> 0
Ex. 311: 3 1 1 3 4 1 -> 0
Ex. 312: 3 1 1 3 4 2 -> 0
                                                      Ex. 410: 332112 -> 1
                           Ex. 361: 3 2 2 1 1 1 -> 1
                           Ex. 362: 3 2 2 1 1 2 -> 1
                                                      Ex. 411: 332121 -> 1
Ex. 313: 3 1 2 1 1 1 -> 1
                                                      Ex. 412: 332122 -> 1
                           Ex. 363: 3 2 2 1 2 1 -> 0
Ex. 314: 3 1 2 1 1 2 -> 1
                                                      Ex. 413: 332131 -> 1
Ex. 315: 3 1 2 1 2 1 -> 0
                           Ex. 364: 3 2 2 1 2 2 -> 0
                                                      Ex. 414: 332132 -> 1
                           Ex. 365: 3 2 2 1 3 1 -> 0
Ex. 316: 312122 -> 0
                           Ex. 366: 322132 -> 0
                                                      Ex. 415: 332141 -> 1
Ex. 317: 3 1 2 1 3 1 -> 0
                                                      Ex. 416: 332142 -> 1
                           Ex. 367: 3 2 2 1 4 1 -> 0
Ex. 318: 3 1 2 1 3 2 -> 0
                                                      Ex. 417: 332211 -> 1
                           Ex. 368: 322142 -> 0
Ex. 319: 3 1 2 1 4 1 -> 0
                           Ex. 369: 3 2 2 2 1 1 -> 1
                                                      Ex. 418: 332212 -> 1
Ex. 320: 3 1 2 1 4 2 -> 0
                           Ex. 370: 322212 -> 1
                                                      Ex. 419: 332221 -> 1
Ex. 321: 3 1 2 2 1 1 -> 1
                                                      Ex. 420: 332222 -> 1
                           Ex. 371: 322221 -> 0
Ex. 322: 3 1 2 2 1 2 -> 1
                           Ex. 372: 3 2 2 2 2 2 -> 0
                                                      Ex. 421: 332231 -> 1
Ex. 323: 3 1 2 2 2 1 -> 0
                                                      Ex. 422: 332232 -> 1
Ex. 324: 312222 -> 0
                           Ex. 373: 322231 -> 0
                           Ex. 374: 322232 -> 0
                                                      Ex. 423: 332241 -> 1
Ex. 325: 3 1 2 2 3 1 -> 0
Ex. 326: 3 1 2 2 3 2 -> 0
                                                      Ex. 424: 332242 -> 1
                           Ex. 375: 322241 -> 0
                           Ex. 376: 322242 -> 0
                                                      Ex. 425: 332311 -> 1
Ex. 327: 3 1 2 2 4 1 -> 0
                                                      Ex. 426: 332312 -> 1
Ex. 328: 312242 -> 0
                           Ex. 377: 3 2 2 3 1 1 -> 1
                                                      Ex. 427: 332321 -> 1
Ex. 329: 3 1 2 3 1 1 -> 1
                           Ex. 378: 3 2 2 3 1 2 -> 1
                           Ex. 379: 3 2 2 3 2 1 -> 0
                                                      Ex. 428: 332322 -> 1
Ex. 330: 3 1 2 3 1 2 -> 1
                           Ex. 380: 3 2 2 3 2 2 -> 0
                                                      Ex. 429: 332331 -> 1
Ex. 331: 3 1 2 3 2 1 -> 0
Ex. 332: 3 1 2 3 2 2 -> 0
                           Ex. 381: 3 2 2 3 3 1 -> 0
                                                      Ex. 430: 332332 -> 1
Ex. 333: 3 1 2 3 3 1 -> 0
                                                      Ex. 431: 332341 -> 1
                           Ex. 382: 3 2 2 3 3 2 -> 0
Ex. 334: 3 1 2 3 3 2 -> 0
                           Ex. 383: 3 2 2 3 4 1 -> 0
                                                      Ex. 432: 332342 -> 1
```

Training Data Set #2

The training set of examples for the second problem: Exactly two of the six attributes have their first value

```
Ex. 117: 131331 -> 0
                                                  Ex. 246: 231132 -> 1
Ex. 4: 111122 -> 0
                                                  Ex. 249: 231211 -> 0
                         Ex. 120: 131342 -> 1
Ex. 7: 111141 -> 0
                                                  Ex. 253: 231231 -> 1
Ex. 9: 111211 -> 0
                         Ex. 125: 132131 -> 0
                         Ex. 126: 132132 -> 1
                                                  Ex. 254: 231232 -> 0
Ex. 10: 111212 -> 0
                         Ex. 127: 132141 -> 0
Ex. 11: 1 1 1 2 2 1 -> 0
                                                  Ex. 256: 231242 -> 0
                                                  Ex. 258: 231312 -> 1
Ex. 13: 111231 -> 0
                         Ex. 130: 132212 -> 1
                                                  Ex. 259: 231321 -> 1
                         Ex. 134: 132232 -> 0
Ex. 15: 111241 -> 0
                                                  Ex. 263: 231341 -> 1
                         Ex. 136: 132242 -> 0
Ex. 19: 1 1 1 3 2 1 -> 0
                                                  Ex. 266: 232112 -> 1
                         Ex. 139: 132321 -> 1
Ex. 23: 111341 -> 0
                                                  Ex. 267: 232121 -> 1
                         Ex. 145: 211111 -> 0
Ex. 25: 112111 -> 0
                         Ex. 148: 211122 -> 0
                                                  Ex. 269: 232131 -> 1
Ex. 26: 112112 -> 0
                                                  Ex. 272: 232142 -> 0
                         Ex. 149: 2 1 1 1 3 1 -> 0
Ex. 37: 112231 -> 0
                         Ex. 156: 211222 -> 1
                                                  Ex. 273: 232211 -> 1
Ex. 39: 112241 -> 0
                         Ex. 162: 211312 -> 0
                                                  Ex. 275: 232221 -> 0
Ex. 40: 112242 -> 1
                         Ex. 164: 211322 -> 1
                                                  Ex. 278: 232232 -> 0
Ex. 42: 112312 -> 0
                         Ex. 166: 211332 -> 1
                                                  Ex. 285: 232331 -> 0
Ex. 44: 112322 -> 1
                                                  Ex. 286: 232332 -> 0
                         Ex. 167: 211341 -> 0
Ex. 50: 121112 -> 0
                                                  Ex. 288: 232342 -> 0
Ex. 58: 121212 -> 0
                         Ex. 169: 212111 -> 0
                         Ex. 172: 212122 -> 1
Ex. 60: 121222 -> 1
                                                  Ex. 295: 311141 -> 0
                                                  Ex. 298: 311212 -> 0
Ex. 61: 121231 -> 0
                         Ex. 175: 212141 -> 0
                                                  Ex. 300: 311222 -> 1
                         Ex. 179: 212221 -> 1
Ex. 62: 121232 -> 1
                         Ex. 184: 212242 -> 0
                                                  Ex. 302: 3 1 1 2 3 2 -> 1
Ex. 63: 121241 -> 0
                                                  Ex. 303: 311241 -> 0
                         Ex. 185: 212311 -> 0
Ex. 65: 121311 -> 0
                                                  Ex. 304: 311242 -> 1
Ex. 66: 121312 -> 0
                         Ex. 186: 212312 -> 1
                         Ex. 188: 212322 -> 0
                                                  Ex. 305: 3 1 1 3 1 1 -> 0
Ex. 68: 121322 -> 1
                         Ex. 190: 212332 -> 0
                                                  Ex. 306: 3 1 1 3 1 2 -> 0
Ex. 69: 121331 -> 0
                                                  Ex. 308: 3 1 1 3 2 2 -> 1
                         Ex. 192: 212342 -> 0
Ex. 70: 121332 -> 1
                                                  Ex. 310: 311332 -> 1
                         Ex. 197: 221131 -> 0
Ex. 71: 121341 -> 0
                                                  Ex. 313: 3 1 2 1 1 1 -> 0
                         Ex. 200: 221142 -> 1
Ex. 72: 121342 -> 1
Ex. 75: 122121 -> 0
                         Ex. 201: 221211 -> 0
                                                  Ex. 316: 312122 -> 1
                         Ex. 205: 221231 -> 1
Ex. 79: 122141 -> 0
                                                  Ex. 317: 312131 -> 0
                                                  Ex. 318: 312132 -> 1
Ex. 85: 122231 -> 1
                         Ex. 213: 221331 -> 1
                         Ex. 214: 221332 -> 0
                                                  Ex. 319: 312141 -> 0
Ex. 87: 122241 -> 1
Ex. 89: 122311 -> 0
                         Ex. 215: 221341 -> 1
                                                  Ex. 320: 3 1 2 1 4 2 -> 1
Ex. 90: 122312 -> 1
                         Ex. 217: 222111 -> 0
                                                  Ex. 323: 3 1 2 2 2 1 -> 1
                         Ex. 220: 2 2 2 1 2 2 -> 0
Ex. 93: 122331 -> 1
                                                  Ex. 330: 312312 -> 1
                         Ex. 222: 2 2 2 1 3 2 -> 0
Ex. 94: 122332 -> 0
                                                  Ex. 331: 312321 -> 1
                                                  Ex. 332: 3 1 2 3 2 2 -> 0
Ex. 95: 122341 -> 1
                         Ex. 223: 2 2 2 1 4 1 -> 1
                         Ex. 224: 222142 -> 0
Ex. 96: 122342 -> 0
                                                  Ex. 336: 312342 -> 0
Ex. 98: 131112 -> 0
                         Ex. 225: 2 2 2 2 1 1 -> 1
                                                  Ex. 338: 3 2 1 1 1 2 -> 0
                         Ex. 228: 2 2 2 2 2 2 -> 0
                                                  Ex. 340: 3 2 1 1 2 2 -> 1
Ex. 100: 131122 -> 0
Ex. 101: 131131 -> 0
                         Ex. 229: 2 2 2 2 3 1 -> 0
                                                  Ex. 341: 3 2 1 1 3 1 -> 0
                         Ex. 233: 222311 -> 1
                                                  Ex. 342: 3 2 1 1 3 2 -> 1
Ex. 102: 131132 -> 0
Ex. 107: 131221 -> 0
                         Ex. 235: 222321 -> 0
                                                  Ex. 346: 3 2 1 2 1 2 -> 1
                                                  Ex. 347: 3 2 1 2 2 1 -> 1
                         Ex. 236: 222322 -> 0
Ex. 108: 131222 -> 1
                         Ex. 240: 222342 -> 0
                                                  Ex. 353: 3 2 1 3 1 1 -> 0
Ex. 110: 131232 -> 1
Ex. 111: 131241 -> 0
                         Ex. 241: 231111 -> 0
                                                  Ex. 355: 3 2 1 3 2 1 -> 1
                                                  Ex. 357: 321331 -> 1
Ex. 116: 131322 -> 1
                         Ex. 242: 231112 -> 0
```

Ex. 358: 321332 -> 0	Ex. 377: 3 2 2 3 1 1 -> 1	Ex. 417: 3 3 2 2 1 1 -> 1
Ex. 361: 3 2 2 1 1 1 -> 0	Ex. 382: 3 2 2 3 3 2 -> 0	Ex. 419: 332221 -> 0
Ex. 364: 3 2 2 1 2 2 -> 0	Ex. 384: 322342 -> 0	Ex. 421: 3 3 2 2 3 1 -> 0
Ex. 365: 3 2 2 1 3 1 -> 1	Ex. 385: 3 3 1 1 1 1 -> 0	Ex. 422: 332232 -> 0
Ex. 366: 3 2 2 1 3 2 -> 0	Ex. 387: 3 3 1 1 2 1 -> 0	Ex. 425: 332311 -> 1
Ex. 369: 3 2 2 2 1 1 -> 1	Ex. 389: 331131 -> 0	Ex. 427: 332321 -> 0
Ex. 371: 3 2 2 2 2 1 -> 0	Ex. 390: 3 3 1 1 3 2 -> 1	Ex. 432: 3 3 2 3 4 2 -> 0
Ex. 372: 3 2 2 2 2 2 -> 0	Ex. 398: 3 3 1 2 3 2 -> 0	
Ex $374 \cdot 322232 \rightarrow 0$	Ex. 409: 332111 -> 0	

Testing Data Set #2

```
Ex. 83: 1 2 2 2 2 1 -> 1
                        Ex. 42: 112312 -> 0
Ex. 1: 111111 -> 0
                                                Ex. 84: 122222 -> 0
                        Ex. 43: 112321 -> 0
Ex. 2: 111112 -> 0
                                                Ex. 85: 122231 -> 1
                        Ex. 44: 112322 -> 1
Ex. 3: 111121 -> 0
                                                Ex. 86: 122232 -> 0
                        Ex. 45: 112331 -> 0
Ex. 4: 111122 -> 0
                                                Ex. 87: 122241 -> 1
Ex. 5: 111131 -> 0
                        Ex. 46: 112332 -> 1
                                                Ex. 88: 122242 -> 0
                        Ex. 47: 112341 -> 0
Ex. 6: 111132 -> 0
                                                Ex. 89: 122311 -> 0
Ex. 7: 111141 -> 0
                        Ex. 48: 112342 -> 1
                                                Ex. 90: 1 2 2 3 1 2 -> 1
Ex. 8: 111142 -> 0
                        Ex. 49: 121111 -> 0
                        Ex. 50: 121112 -> 0
                                                Ex. 91: 122321 -> 1
Ex. 9: 111211 -> 0
                                                Ex. 92: 122322 \rightarrow 0
                        Ex. 51: 121121 -> 0
Ex. 10: 111212 -> 0
                                                Ex. 93: 122331 -> 1
                        Ex. 52: 121122 -> 0
Ex. 11: 111221 -> 0
                                                Ex. 94: 122332 -> 0
                        Ex. 53: 121131 -> 0
Ex. 12: 111222 -> 0
                                                Ex. 95: 122341 -> 1
                        Ex. 54: 121132 -> 0
Ex. 13: 111231 -> 0
                                                Ex. 96: 122342 -> 0
Ex. 14: 111232 -> 0
                        Ex. 55: 121141 -> 0
Ex. 15: 111241 -> 0
                        Ex. 56: 121142 -> 0
                                                Ex. 97: 131111 -> 0
Ex. 16: 111242 -> 0
                        Ex. 57: 121211 -> 0
                                                Ex. 98: 131112 -> 0
                        Ex. 58: 121212 -> 0
                                                Ex. 99: 131121 -> 0
Ex. 17: 111311 -> 0
                                                Ex. 100: 131122 -> 0
                        Ex. 59: 121221 -> 0
Ex. 18: 111312 -> 0
                                                Ex. 101: 131131 -> 0
                        Ex. 60: 121222 -> 1
Ex. 19: 111321 -> 0
                                                Ex. 102: 131132 -> 0
                        Ex. 61: 121231 -> 0
Ex. 20: 111322 -> 0
                        Ex. 62: 121232 -> 1
                                                Ex. 103: 131141 -> 0
Ex. 21: 111331 -> 0
                        Ex. 63: 121241 -> 0
                                                Ex. 104: 131142 -> 0
Ex. 22: 111332 -> 0
                                                Ex. 105: 131211 -> 0
                        Ex. 64: 121242 -> 1
Ex. 23: 111341 -> 0
                                                Ex. 106: 131212 -> 0
Ex. 24: 111342 -> 0
                        Ex. 65: 121311 -> 0
                        Ex. 66: 121312 -> 0
                                                Ex. 107: 131221 -> 0
Ex. 25: 112111 -> 0
Ex. 26: 112112 -> 0
                        Ex. 67: 121321 -> 0
                                                Ex. 108: 131222 -> 1
                        Ex. 68: 121322 -> 1
                                                 Ex. 109: 131231 -> 0
Ex. 27: 112121 -> 0
                                                Ex. 110: 131232 -> 1
                        Ex. 69: 121331 -> 0
Ex. 28: 112122 -> 0
Ex. 29: 112131 -> 0
                        Ex. 70: 121332 -> 1
                                                Ex. 111: 131241 -> 0
                                                Ex. 112: 131242 -> 1
                        Ex. 71: 121341 -> 0
Ex. 30: 112132 -> 0
                        Ex. 72: 121342 -> 1
                                                Ex. 113: 131311 -> 0
Ex. 31: 112141 -> 0
                        Ex. 73: 122111 -> 0
                                                Ex. 114: 131312 -> 0
Ex. 32: 112142 -> 0
                        Ex. 74: 122112 -> 0
                                                 Ex. 115: 131321 -> 0
Ex. 33: 112211 -> 0
                                                Ex. 116: 131322 -> 1
                        Ex. 75: 122121 -> 0
Ex. 34: 112212 -> 0
                        Ex. 76: 122122 -> 1
                                                Ex. 117: 131331 -> 0
Ex. 35: 112221 -> 0
                                                Ex. 118: 131332 -> 1
                        Ex. 77: 122131 -> 0
Ex. 36: 112222 -> 1
                                                Ex. 119: 131341 -> 0
Ex. 37: 112231 -> 0
                        Ex. 78: 122132 -> 1
                        Ex. 79: 122141 -> 0
                                                 Ex. 120: 131342 -> 1
Ex. 38: 112232 -> 1
                        Ex. 80: 122142 -> 1
                                                Ex. 121: 132111 -> 0
Ex. 39: 112241 -> 0
                                                Ex. 122: 132112 -> 0
                        Ex. 81: 122211 -> 0
Ex. 40: 112242 -> 1
                                                 Ex. 123: 132121 -> 0
Ex. 41: 112311 -> 0
                        Ex. 82: 1 2 2 2 1 2 -> 1
```

```
Ex. 178: 212212 -> 1
                                                 Ex. 232: 222242 -> 0
Ex. 124: 132122 -> 1
                                                 Ex. 233: 222311 -> 1
                        Ex. 179: 212221 -> 1
Ex. 125: 132131 -> 0
                                                 Ex. 234: 222312 -> 0
                        Ex. 180: 212222 -> 0
Ex. 126: 132132 -> 1
                        Ex. 181: 212231 -> 1
                                                 Ex. 235: 222321 -> 0
Ex. 127: 132141 -> 0
                                                 Ex. 236: 222322 -> 0
                        Ex. 182: 212232 -> 0
Ex. 128: 132142 -> 1
                        Ex. 183: 212241 -> 1
                                                 Ex. 237: 222331 -> 0
Ex. 129: 132211 -> 0
                                                 Ex. 238: 222332 -> 0
                        Ex. 184: 212242 -> 0
Ex. 130: 132212 -> 1
                                                 Ex. 239: 222341 -> 0
                        Ex. 185: 212311 -> 0
Ex. 131: 132221 -> 1
                                                 Ex. 240: 222342 -> 0
                        Ex. 186: 212312 -> 1
Ex. 132: 132222 -> 0
                                                 Ex. 241: 231111 -> 0
                        Ex. 187: 212321 -> 1
Ex. 133: 132231 -> 1
                                                 Ex. 242: 231112 -> 0
                        Ex. 188: 212322 -> 0
Ex. 134: 132232 -> 0
                                                 Ex. 243: 231121 -> 0
                        Ex. 189: 212331 -> 1
Ex. 135: 132241 -> 1
Ex. 136: 132242 -> 0
                                                 Ex. 244: 231122 -> 1
                        Ex. 190: 212332 -> 0
                                                 Ex. 245: 231131 -> 0
                        Ex. 191: 212341 -> 1
Ex. 137: 132311 -> 0
                                                 Ex. 246: 231132 -> 1
                        Ex. 192: 212342 -> 0
Ex. 138: 132312 -> 1
                        Ex. 193: 221111 -> 0
                                                 Ex. 247: 231141 -> 0
Ex. 139: 132321 -> 1
                                                 Ex. 248: 231142 -> 1
Ex. 140: 132322 -> 0
                        Ex. 194: 221112 -> 0
                                                 Ex. 249: 231211 -> 0
                        Ex. 195: 221121 -> 0
Ex. 141: 132331 -> 1
                                                 Ex. 250: 231212 -> 1
                        Ex. 196: 221122 -> 1
Ex. 142: 132332 -> 0
                                                 Ex. 251: 231221 -> 1
                        Ex. 197: 221131 -> 0
Ex. 143: 132341 -> 1
                                                 Ex. 252: 231222 -> 0
                        Ex. 198: 221132 -> 1
Ex. 144: 132342 -> 0
                                                 Ex. 253: 231231 -> 1
                        Ex. 199: 221141 -> 0
Ex. 145: 211111 -> 0
                                                 Ex. 254: 231232 -> 0
                        Ex. 200: 221142 -> 1
Ex. 146: 211112 -> 0
                                                 Ex. 255: 231241 -> 1
                        Ex. 201: 221211 -> 0
Ex. 147: 211121 -> 0
                        Ex. 202: 2 2 1 2 1 2 -> 1
                                                 Ex. 256: 231242 -> 0
Ex. 148: 211122 -> 0
                                                 Ex. 257: 231311 -> 0
                        Ex. 203: 221221 -> 1
Ex. 149: 211131 -> 0
                        Ex. 204: 221222 -> 0
                                                 Ex. 258: 231312 -> 1
Ex. 150: 211132 -> 0
                                                 Ex. 259: 231321 -> 1
                        Ex. 205: 221231 -> 1
Ex. 151: 211141 -> 0
                                                 Ex. 260: 231322 -> 0
                        Ex. 206: 221232 -> 0
Ex. 152: 211142 -> 0
                        Ex. 207: 221241 -> 1
                                                 Ex. 261: 231331 -> 1
Ex. 153: 2 1 1 2 1 1 -> 0
                                                 Ex. 262: 231332 -> 0
                        Ex. 208: 221242 -> 0
Ex. 154: 211212 -> 0
                                                 Ex. 263: 231341 -> 1
                        Ex. 209: 221311 -> 0
Ex. 155: 211221 -> 0
                        Ex. 210: 221312 -> 1
                                                 Ex. 264: 231342 -> 0
Ex. 156: 211222 -> 1
                                                 Ex. 265: 232111 -> 0
Ex. 157: 2 1 1 2 3 1 -> 0
                        Ex. 211: 221321 -> 1
                                                 Ex. 266: 232112 -> 1
                        Ex. 212: 221322 -> 0
Ex. 158: 211232 -> 1
                                                 Ex. 267: 232121 -> 1
                        Ex. 213: 221331 -> 1
Ex. 159: 211241 -> 0
                                                 Ex. 268: 232122 -> 0
                        Ex. 214: 221332 -> 0
Ex. 160: 211242 -> 1
                                                 Ex. 269: 232131 -> 1
Ex. 161: 211311 -> 0
                        Ex. 215: 221341 -> 1
                                                 Ex. 270: 232132 -> 0
                        Ex. 216: 221342 -> 0
Ex. 162: 2 1 1 3 1 2 -> 0
                                                 Ex. 271: 232141 -> 1
                        Ex. 217: 222111 -> 0
Ex. 163: 211321 -> 0
                        Ex. 218: 222112 -> 1
                                                 Ex. 272: 232142 -> 0
Ex. 164: 211322 -> 1
                                                 Ex. 273: 232211 -> 1
                        Ex. 219: 222121 -> 1
Ex. 165: 211331 -> 0
                                                 Ex. 274: 232212 -> 0
                        Ex. 220: 2 2 2 1 2 2 -> 0
Ex. 166: 211332 -> 1
                                                 Ex. 275: 232221 -> 0
                        Ex. 221: 2 2 2 1 3 1 -> 1
Ex. 167: 211341 -> 0
                                                 Ex. 276: 232222 -> 0
Ex. 168: 211342 -> 1
                        Ex. 222: 2 2 2 1 3 2 -> 0
                                                 Ex. 277: 232231 -> 0
Ex. 169: 212111 -> 0
                        Ex. 223: 2 2 2 1 4 1 -> 1
                        Ex. 224: 222142 -> 0
                                                 Ex. 278: 232232 -> 0
Ex. 170: 212112 -> 0
                                                 Ex. 279: 232241 -> 0
Ex. 171: 212121 -> 0
                        Ex. 225: 2 2 2 2 1 1 -> 1
                                                 Ex. 280: 232242 -> 0
Ex. 172: 212122 -> 1
                        Ex. 226: 222212 -> 0
                                                 Ex. 281: 232311 -> 1
                        Ex. 227: 22221 -> 0
Ex. 173: 2 1 2 1 3 1 -> 0
                        Ex. 228: 22222 -> 0
                                                 Ex. 282: 232312 -> 0
Ex. 174: 212132 -> 1
                        Ex. 229: 222231 -> 0
                                                 Ex. 283: 232321 -> 0
Ex. 175: 212141 -> 0
                                                 Ex. 284: 232322 -> 0
                        Ex. 230: 222232 -> 0
Ex. 176: 212142 -> 1
                        Ex. 231: 222241 -> 0
                                                 Ex. 285: 232331 -> 0
Ex. 177: 212211 -> 0
```

```
Ex. 384: 322342 -> 0
Ex. 286: 232332 -> 0
                          Ex. 335: 312341 -> 1
                          Ex. 336: 312342 -> 0
                                                     Ex. 385: 3 3 1 1 1 1 -> 0
Ex. 287: 232341 -> 0
                          Ex. 337: 3 2 1 1 1 1 -> 0
                                                     Ex. 386: 331112 -> 0
Ex. 288: 232342 -> 0
                          Ex. 338: 3 2 1 1 1 2 -> 0
                                                     Ex. 387: 331121 -> 0
Ex. 289: 311111 -> 0
                          Ex. 339: 3 2 1 1 2 1 -> 0
                                                     Ex. 388: 3 3 1 1 2 2 -> 1
Ex. 290: 3 1 1 1 1 2 -> 0
                          Ex. 340: 321122 -> 1
                                                     Ex. 389: 3 3 1 1 3 1 -> 0
Ex. 291: 311121 -> 0
                          Ex. 341: 321131 -> 0
                                                     Ex. 390: 3 3 1 1 3 2 -> 1
Ex. 292: 3 1 1 1 2 2 -> 0
Ex. 293: 311131 -> 0
                          Ex. 342: 3 2 1 1 3 2 -> 1
                                                     Ex. 391: 331141 -> 0
                          Ex. 343: 3 2 1 1 4 1 -> 0
                                                     Ex. 392: 3 3 1 1 4 2 -> 1
Ex. 294: 311132 -> 0
                          Ex. 344: 321142 -> 1
                                                     Ex. 393: 3 3 1 2 1 1 -> 0
Ex. 295: 311141 -> 0
                                                    Ex. 394: 331212 -> 1
                          Ex. 345: 3 2 1 2 1 1 -> 0
Ex. 296: 311142 -> 0
                          Ex. 346: 321212 -> 1
                                                    Ex. 395: 3 3 1 2 2 1 -> 1
Ex. 297: 3 1 1 2 1 1 -> 0
                          Ex. 347: 321221 -> 1
                                                    Ex. 396: 331222 -> 0
Ex. 298: 3 1 1 2 1 2 -> 0
                                                     Ex. 397: 331231 -> 1
                          Ex. 348: 321222 -> 0
Ex. 299: 3 1 1 2 2 1 -> 0
                          Ex. 349: 3 2 1 2 3 1 -> 1
Ex. 300: 3 1 1 2 2 2 -> 1
                                                     Ex. 398: 331232 -> 0
                                                    Ex. 399: 331241 -> 1
Ex. 301: 3 1 1 2 3 1 -> 0
                          Ex. 350: 321232 -> 0
                                                     Ex. 400: 331242 -> 0
                          Ex. 351: 321241 -> 1
Ex. 302: 3 1 1 2 3 2 -> 1
                          Ex. 352: 3 2 1 2 4 2 -> 0
                                                     Ex. 401: 331311 -> 0
Ex. 303: 3 1 1 2 4 1 -> 0
                          Ex. 353: 3 2 1 3 1 1 -> 0
                                                    Ex. 402: 331312 -> 1
Ex. 304: 311242 -> 1
                                                    Ex. 403: 331321 -> 1
                          Ex. 354: 3 2 1 3 1 2 -> 1
Ex. 305: 3 1 1 3 1 1 -> 0
                                                    Ex. 404: 331322 -> 0
Ex. 306: 311312 -> 0
                          Ex. 355: 321321 -> 1
                                                    Ex. 405: 331331 -> 1
                          Ex. 356: 321322 -> 0
Ex. 307: 3 1 1 3 2 1 -> 0
                                                    Ex. 406: 331332 -> 0
Ex. 308: 311322 -> 1
                          Ex. 357: 321331 -> 1
Ex. 309: 3 1 1 3 3 1 -> 0
                          Ex. 358: 321332 -> 0
                                                    Ex. 407: 331341 -> 1
                          Ex. 359: 321341 -> 1
                                                    Ex. 408: 331342 -> 0
Ex. 310: 311332 -> 1
                                                    Ex. 409: 332111 -> 0
Ex. 311: 3 1 1 3 4 1 -> 0
                          Ex. 360: 321342 -> 0
                          Ex. 361: 3 2 2 1 1 1 -> 0
                                                    Ex. 410: 332112 -> 1
Ex. 312: 311342 -> 1
Ex. 313: 3 1 2 1 1 1 -> 0
                                                    Ex. 411: 332121 -> 1
                          Ex. 362: 3 2 2 1 1 2 -> 1
                          Ex. 363: 3 2 2 1 2 1 -> 1
                                                    Ex. 412: 332122 -> 0
Ex. 314: 312112 -> 0
                          Ex. 364: 322122 -> 0
                                                    Ex. 413: 332131 -> 1
Ex. 315: 3 1 2 1 2 1 -> 0
                          Ex. 365: 3 2 2 1 3 1 -> 1
                                                    Ex. 414: 332132 -> 0
Ex. 316: 3 1 2 1 2 2 -> 1
                                                    Ex. 415: 332141 -> 1
                          Ex. 366: 322132 -> 0
Ex. 317: 3 1 2 1 3 1 -> 0
                          Ex. 367: 3 2 2 1 4 1 -> 1
                                                    Ex. 416: 332142 -> 0
Ex. 318: 312132 -> 1
                          Ex. 368: 322142 -> 0
                                                    Ex. 417: 332211 -> 1
Ex. 319: 3 1 2 1 4 1 -> 0
Ex. 320: 3 1 2 1 4 2 -> 1
                          Ex. 369: 3 2 2 2 1 1 -> 1
                                                    Ex. 418: 332212 -> 0
Ex. 321: 3 1 2 2 1 1 -> 0
                          Ex. 370: 3 2 2 2 1 2 -> 0
                                                    Ex. 419: 332221 -> 0
                          Ex. 371: 322221 -> 0
                                                    Ex. 420: 332222 -> 0
Ex. 322: 3 1 2 2 1 2 -> 1
Ex. 323: 312221 -> 1
                          Ex. 372: 322222 -> 0
                                                    Ex. 421: 332231 -> 0
Ex. 324: 3 1 2 2 2 2 -> 0
                          Ex. 373: 3 2 2 2 3 1 -> 0
                                                    Ex. 422: 332232 -> 0
                          Ex. 374: 322232 -> 0
                                                    Ex. 423: 332241 -> 0
Ex. 325: 312231 -> 1
Ex. 326: 3 1 2 2 3 2 -> 0
                                                    Ex. 424: 332242 -> 0
                          Ex. 375: 3 2 2 2 4 1 -> 0
                          Ex. 376: 322242 -> 0
Ex. 327: 312241 -> 1
                                                    Ex. 425: 332311 -> 1
                          Ex. 377: 3 2 2 3 1 1 -> 1
Ex. 328: 312242 -> 0
                                                    Ex. 426: 332312 -> 0
                                                    Ex. 427: 332321 -> 0
Ex. 329: 312311 -> 0
                          Ex. 378: 3 2 2 3 1 2 -> 0
                          Ex. 379: 3 2 2 3 2 1 -> 0
                                                    Ex. 428: 332322 -> 0
Ex. 330: 312312 -> 1
                                                    Ex. 429: 332331 -> 0
                          Ex. 380: 322322 -> 0
Ex. 331: 312321 -> 1
                                                    Ex. 430: 332332 -> 0
Ex. 332: 3 1 2 3 2 2 -> 0
                          Ex. 381: 3 2 2 3 3 1 -> 0
Ex. 333: 312331 -> 1
                          Ex. 382: 3 2 2 3 3 2 -> 0
                                                    Ex. 431: 332341 -> 0
                                                    Ex. 432: 332342 -> 0
                          Ex. 383: 3 2 2 3 4 1 -> 0
Ex. 334: 312332 -> 0
```

Training Data Set #3

The training set of examples for the third problem with noisy data: (jacket_color is green and holding is sword) or (jacket_color is not blue and body shape is not octagon)

```
Ex. 271: 232141 -> 0
                         Ex. 121: 132111 -> 0
Ex. 2: 1111112 -> 1
                                                  Ex. 277: 232231 -> 0
                         Ex. 122: 132112 -> 0
Ex. 3: 111121 -> 1
                                                  Ex. 280: 232242 \rightarrow 0
                         Ex. 123: 132121 -> 0
Ex. 4: 111122 -> 1
                                                  Ex. 281: 232311 -> 0
Ex. 5: 111131 -> 0
                         Ex. 128: 132142 -> 0
                                                  Ex. 283: 232321 -> 0
                         Ex. 134: 132232 -> 0
Ex. 7: 111141 -> 0
                                                  Ex. 288: 232342 -> 0
Ex. 9: 111211 -> 1
                         Ex. 136: 132242 -> 0
                                                  Ex. 289: 311111 -> 1
                         Ex. 143: 132341 -> 0
Ex. 12: 1 1 1 2 2 2 -> 1
                                                  Ex. 291: 311121 -> 1
Ex. 16: 111242 -> 0
                         Ex. 145: 2 1 1 1 1 1 -> 1
Ex. 28: 112122 -> 1
                         Ex. 146: 211112 -> 1
                                                  Ex. 293: 311131 -> 1
                                                  Ex. 304: 311242 -> 0
                         Ex. 151: 211141 -> 0
Ex. 32: 112142 -> 0
                                                  Ex. 306: 311312 -> 1
                         Ex. 152: 211142 -> 0
Ex. 36: 112222 -> 1
                                                  Ex. 312: 311342 -> 0
Ex. 39: 112241 -> 0
                         Ex. 153: 211211 -> 1
                                                  Ex. 315: 312121 -> 1
Ex. 40: 112242 -> 0
                         Ex. 154: 211212 -> 1
                                                  Ex. 326: 312232 -> 1
                         Ex. 164: 211322 -> 1
Ex. 41: 112311 -> 1
                         Ex. 166: 211332 -> 1
                                                  Ex. 328: 312242 -> 0
Ex. 42: 112312 -> 1
                                                  Ex. 329: 3 1 2 3 1 1 -> 1
                         Ex. 167: 211341 -> 0
Ex. 45: 112331 -> 1
                                                  Ex. 340: 3 2 1 1 2 2 -> 1
                         Ex. 172: 212122 -> 1
Ex. 46: 112332 -> 1
                                                  Ex. 343: 3 2 1 1 4 1 -> 0
Ex. 53: 121131 -> 1
                         Ex. 183: 212241 -> 0
Ex. 59: 121221 -> 1
                         Ex. 186: 212312 -> 1
                                                  Ex. 349: 321231 -> 1
                                                  Ex. 354: 321312 -> 1
Ex. 60: 121222 -> 1
                         Ex. 198: 221132 -> 1
                         Ex. 200: 221142 -> 0
                                                  Ex. 364: 3 2 2 1 2 2 -> 1
Ex. 61: 121231 -> 0
                         Ex. 202: 221212 -> 1
                                                  Ex. 366: 3 2 2 1 3 2 -> 1
Ex. 65: 121311 -> 1
                                                  Ex. 370: 3 2 2 2 1 2 -> 1
                         Ex. 203: 221221 -> 0
Ex. 66: 121312 -> 1
                                                  Ex. 377: 3 2 2 3 1 1 -> 1
                         Ex. 209: 221311 -> 1
Ex. 67: 121321 -> 1
                         Ex. 212: 221322 -> 1
                                                  Ex. 382: 3 2 2 3 3 2 -> 1
Ex. 68: 121322 -> 1
                                                  Ex. 383: 3 2 2 3 4 1 -> 0
Ex. 70: 121332 -> 1
                         Ex. 213: 221331 -> 0
                                                  Ex. 390: 331132 -> 1
Ex. 71: 121341 -> 0
                         Ex. 214: 221332 -> 0
                                                  Ex. 391: 3 3 1 1 4 1 -> 1
                         Ex. 216: 221342 -> 0
Ex. 77: 122131 -> 1
Ex. 80: 122142 -> 0
                         Ex. 220: 2 2 2 1 2 2 -> 1
                                                  Ex. 400: 331242 -> 0
                         Ex. 226: 222212 -> 1
                                                  Ex. 401: 331311 -> 0
Ex. 81: 122211 -> 1
                                                  Ex. 403: 331321 -> 0
                         Ex. 229: 222231 -> 1
Ex. 83: 122221 -> 1
                         Ex. 230: 222232 -> 1
                                                  Ex. 404: 331322 -> 0
Ex. 84: 122222 -> 1
                                                  Ex. 407: 331341 -> 0
                         Ex. 239: 222341 -> 0
Ex. 89: 122311 -> 1
Ex. 91: 122321 -> 1
                         Ex. 245: 231131 -> 1
                                                  Ex. 409: 332111 -> 0
                                                  Ex. 410: 332112 -> 0
Ex. 92: 122322 -> 1
                         Ex. 249: 231211 -> 0
                         Ex. 251: 231221 -> 0
Ex. 99: 131121 -> 0
                                                  Ex. 420: 332222 -> 0
                         Ex. 252: 231222 -> 0
                                                  Ex. 422: 332232 -> 0
Ex. 103: 131141 -> 0
Ex. 110: 131232 -> 0
                                                  Ex. 425: 332311 -> 0
                         Ex. 254: 231232 -> 0
                         Ex. 261: 231331 -> 0
                                                  Ex. 430: 332332 -> 0
Ex. 111: 131241 -> 0
                         Ex. 266: 232112 -> 0
                                                  Ex. 432: 332342 -> 0
Ex. 113: 131311 -> 0
Ex. 117: 131331 -> 0
                         Ex. 268: 232122 -> 0
```

Testing Data Set #3

```
Ex. 52: 121122 -> 1
                                                 Ex. 103: 131141 -> 0
Ex. 1: 111111 -> 1
                                                 Ex. 104: 131142 -> 0
                        Ex. 53: 121131 -> 1
Ex. 2: 111112 -> 1
                        Ex. 54: 121132 -> 1
                                                 Ex. 105: 131211 -> 0
Ex. 3: 111121 -> 1
                        Ex. 55: 121141 -> 0
                                                 Ex. 106: 131212 -> 0
Ex. 4: 111122 -> 1
                                                 Ex. 107: 131221 -> 0
                        Ex. 56: 121142 -> 0
Ex. 5: 111131 -> 1
                                                Ex. 108: 131222 -> 0
                        Ex. 57: 121211 -> 1
Ex. 6: 111132 -> 1
                        Ex. 58: 121212 -> 1
                                                Ex. 109: 131231 -> 0
Ex. 7: 111141 -> 0
                        Ex. 59: 121221 -> 1
                                                 Ex. 110: 131232 -> 0
Ex. 8: 111142 -> 0
                                                Ex. 111: 131241 -> 0
Ex. 9: 111211 -> 1
                        Ex. 60: 121222 -> 1
                        Ex. 61: 121231 -> 1
                                                 Ex. 112: 131242 -> 0
Ex. 10: 111212 -> 1
Ex. 11: 111221 -> 1
                                                 Ex. 113: 131311 -> 0
                        Ex. 62: 121232 -> 1
                                                Ex. 114: 131312 -> 0
                        Ex. 63: 121241 -> 0
Ex. 12: 111222 -> 1
                        Ex. 64: 121242 -> 0
                                                Ex. 115: 131321 -> 0
Ex. 13: 111231 -> 1
                                                Ex. 116: 131322 -> 0
Ex. 14: 111232 -> 1
                        Ex. 65: 121311 -> 1
                                                Ex. 117: 131331 -> 0
Ex. 15: 111241 -> 0
                        Ex. 66: 121312 -> 1
                        Ex. 67: 121321 -> 1
                                                 Ex. 118: 131332 -> 0
Ex. 16: 111242 -> 0
                                                 Ex. 119: 131341 -> 0
Ex. 17: 1 1 1 3 1 1 -> 1
                        Ex. 68: 121322 -> 1
                        Ex. 69: 121331 -> 1
                                                Ex. 120: 131342 -> 0
Ex. 18: 111312 -> 1
                        Ex. 70: 121332 -> 1
                                                 Ex. 121: 132111 -> 0
Ex. 19: 111321 -> 1
                                                 Ex. 122: 132112 -> 0
                        Ex. 71: 121341 -> 0
Ex. 20: 111322 -> 1
                                                 Ex. 123: 132121 -> 0
                        Ex. 72: 121342 -> 0
Ex. 21: 111331 -> 1
                                                Ex. 124: 132122 -> 0
Ex. 22: 111332 -> 1
                        Ex. 73: 122111 -> 1
                        Ex. 74: 122112 -> 1
                                                 Ex. 125: 132131 -> 1
Ex. 23: 111341 -> 0
Ex. 24: 111342 -> 0
                        Ex. 75: 122121 -> 1
                                                 Ex. 126: 132132 -> 1
                                                 Ex. 127: 132141 -> 0
                        Ex. 76: 122122 -> 1
Ex. 25: 112111 -> 1
                        Ex. 77: 122131 -> 1
                                                 Ex. 128: 132142 -> 0
Ex. 26: 112112 -> 1
                                                 Ex. 129: 132211 -> 0
                        Ex. 78: 122132 -> 1
Ex. 27: 112121 -> 1
                                                 Ex. 130: 132212 -> 0
Ex. 28: 112122 -> 1
                        Ex. 79: 122141 -> 0
                                                 Ex. 131: 132221 -> 0
Ex. 29: 112131 -> 1
                        Ex. 80: 122142 -> 0
                                                 Ex. 132: 132222 -> 0
                        Ex. 81: 122211 -> 1
Ex. 30: 112132 -> 1
                        Ex. 82: 122212 -> 1
                                                 Ex. 133: 132231 -> 0
Ex. 31: 112141 -> 0
Ex. 32: 112142 -> 0
                        Ex. 83: 122221 -> 1
                                                 Ex. 134: 132232 -> 0
                                                 Ex. 135: 132241 -> 0
                        Ex. 84: 122222 -> 1
Ex. 33: 112211 -> 1
                        Ex. 85: 122231 -> 1
                                                 Ex. 136: 132242 -> 0
Ex. 34: 112212 -> 1
Ex. 35: 112221 -> 1
                        Ex. 86: 122232 -> 1
                                                 Ex. 137: 132311 -> 0
                        Ex. 87: 122241 -> 0
                                                 Ex. 138: 132312 -> 0
Ex. 36: 112222 -> 1
                                                 Ex. 139: 132321 -> 0
Ex. 37: 112231 -> 1
                        Ex. 88: 122242 -> 0
                                                 Ex. 140: 132322 -> 0
                        Ex. 89: 122311 -> 1
Ex. 38: 112232 -> 1
                        Ex. 90: 122312 -> 1
                                                 Ex. 141: 132331 -> 0
Ex. 39: 112241 -> 0
                        Ex. 91: 122321 -> 1
                                                 Ex. 142: 132332 -> 0
Ex. 40: 112242 -> 0
                                                 Ex. 143: 132341 -> 0
Ex. 41: 112311 -> 1
                        Ex. 92: 122322 -> 1
                                                 Ex. 144: 132342 -> 0
Ex. 42: 112312 -> 1
                        Ex. 93: 122331 -> 1
                        Ex. 94: 122332 -> 1
                                                 Ex. 145: 2 1 1 1 1 1 -> 1
Ex. 43: 112321 -> 1
                                                 Ex. 146: 211112 -> 1
Ex. 44: 112322 -> 1
                        Ex. 95: 122341 -> 0
Ex. 45: 112331 -> 1
                        Ex. 96: 122342 -> 0
                                                 Ex. 147: 2 1 1 1 2 1 -> 1
                                                Ex. 148: 211122 -> 1
                        Ex. 97: 131111 -> 0
Ex. 46: 112332 -> 1
                                                 Ex. 149: 211131 -> 1
                        Ex. 98: 131112 -> 0
Ex. 47: 112341 -> 0
Ex. 48: 112342 -> 0
                        Ex. 99: 131121 -> 0
                                                 Ex. 150: 211132 -> 1
                                                 Ex. 151: 211141 -> 0
                        Ex. 100: 131122 -> 0
Ex. 49: 121111 -> 1
                                                 Ex. 152: 211142 -> 0
                        Ex. 101: 131131 -> 1
Ex. 50: 121112 -> 1
                                                 Ex. 153: 211211 -> 1
Ex. 51: 121121 -> 1
                        Ex. 102: 131132 -> 1
```

```
Ex. 262: 231332 -> 0
                        Ex. 208: 221242 -> 0
Ex. 154: 211212 -> 1
                        Ex. 209: 221311 -> 1
                                                 Ex. 263: 231341 -> 0
Ex. 155: 211221 -> 1
                                                 Ex. 264: 231342 -> 0
Ex. 156: 211222 -> 1
                        Ex. 210: 221312 -> 1
                        Ex. 211: 221321 -> 1
                                                 Ex. 265: 232111 -> 0
Ex. 157: 211231 -> 1
                        Ex. 212: 221322 -> 1
                                                 Ex. 266: 232112 -> 0
Ex. 158: 211232 -> 1
Ex. 159: 211241 -> 0
                        Ex. 213: 221331 -> 1
                                                 Ex. 267: 232121 -> 0
                        Ex. 214: 221332 -> 1
                                                 Ex. 268: 232122 -> 0
Ex. 160: 211242 -> 0
                        Ex. 215: 221341 -> 0
                                                 Ex. 269: 232131 -> 1
Ex. 161: 211311 -> 1
                                                 Ex. 270: 232132 -> 1
Ex. 162: 211312 -> 1
                        Ex. 216: 221342 -> 0
                        Ex. 217: 222111 -> 1
                                                 Ex. 271: 232141 -> 0
Ex. 163: 211321 -> 1
                                                 Ex. 272: 232142 -> 0
                        Ex. 218: 222112 -> 1
Ex. 164: 211322 -> 1
                                                 Ex. 273: 232211 -> 0
Ex. 165: 211331 -> 1
                        Ex. 219: 222121 -> 1
                        Ex. 220: 222122 -> 1
                                                 Ex. 274: 232212 -> 0
Ex. 166: 211332 -> 1
                        Ex. 221: 222131 -> 1
                                                 Ex. 275: 232221 -> 0
Ex. 167: 211341 -> 0
                                                 Ex. 276: 232222 -> 0
                        Ex. 222: 222132 -> 1
Ex. 168: 211342 -> 0
                                                 Ex. 277: 232231 -> 0
                        Ex. 223: 222141 -> 0
Ex. 169: 212111 -> 1
                                                 Ex. 278: 232232 -> 0
                        Ex. 224: 222142 -> 0
Ex. 170: 212112 -> 1
                        Ex. 225: 222211 -> 1
                                                 Ex. 279: 232241 -> 0
Ex. 171: 212121 -> 1
                                                 Ex. 280: 232242 -> 0
                        Ex. 226: 222212 -> 1
Ex. 172: 212122 -> 1
                                                 Ex. 281: 232311 -> 0
                        Ex. 227: 22221 -> 1
Ex. 173: 212131 -> 1
                        Ex. 228: 22222 -> 1
                                                 Ex. 282: 232312 -> 0
Ex. 174: 212132 -> 1
                                                 Ex. 283: 232321 -> 0
                        Ex. 229: 2 2 2 2 3 1 -> 1
Ex. 175: 212141 -> 0
                                                 Ex. 284: 232322 -> 0
                        Ex. 230: 222232 -> 1
Ex. 176: 212142 -> 0
                                                 Ex. 285: 232331 -> 0
                        Ex. 231: 222241 -> 0
Ex. 177: 212211 -> 1
                                                 Ex. 286: 232332 -> 0
                         Ex. 232: 222242 -> 0
Ex. 178: 212212 -> 1
                                                 Ex. 287: 232341 -> 0
                        Ex. 233: 222311 -> 1
Ex. 179: 212221 -> 1
                                                 Ex. 288: 232342 -> 0
                        Ex. 234: 222312 -> 1
Ex. 180: 212222 -> 1
                                                 Ex. 289: 311111 -> 1
Ex. 181: 212231 -> 1
                        Ex. 235: 222321 -> 1
                                                 Ex. 290: 3 1 1 1 1 2 -> 1
                        Ex. 236: 222322 -> 1
Ex. 182: 212232 -> 1
                         Ex. 237: 222331 -> 1
                                                 Ex. 291: 3 1 1 1 2 1 -> 1
Ex. 183: 212241 -> 0
Ex. 184: 212242 -> 0
                         Ex. 238: 222332 -> 1
                                                 Ex. 292: 311122 -> 1
                                                 Ex. 293: 3 1 1 1 3 1 -> 1
                         Ex. 239: 222341 -> 0
Ex. 185: 212311 -> 1
                         Ex. 240: 222342 -> 0
                                                 Ex. 294: 311132 -> 1
Ex. 186: 212312 -> 1
                                                 Ex. 295: 311141 -> 0
                         Ex. 241: 231111 -> 0
Ex. 187: 212321 -> 1
                         Ex. 242: 231112 -> 0
                                                 Ex. 296: 311142 -> 0
Ex. 188: 212322 -> 1
                                                 Ex. 297: 311211 -> 1
                         Ex. 243: 231121 -> 0
Ex. 189: 212331 -> 1
                                                 Ex. 298: 311212 -> 1
Ex. 190: 212332 -> 1
                         Ex. 244: 231122 -> 0
                         Ex. 245: 231131 -> 1
                                                 Ex. 299: 311221 -> 1
Ex. 191: 212341 -> 0
                                                 Ex. 300: 311222 -> 1
Ex. 192: 212342 -> 0
                         Ex. 246: 231132 -> 1
                         Ex. 247: 231141 -> 0
                                                 Ex. 301: 3 1 1 2 3 1 -> 1
Ex. 193: 221111 -> 1
Ex. 194: 221112 -> 1
                                                 Ex. 302: 3 1 1 2 3 2 -> 1
                         Ex. 248: 231142 -> 0
                                                 Ex. 303: 311241 -> 0
                         Ex. 249: 231211 -> 0
Ex. 195: 221121 -> 1
                                                 Ex. 304: 311242 -> 0
                         Ex. 250: 231212 -> 0
Ex. 196: 221122 -> 1
                                                 Ex. 305: 3 1 1 3 1 1 -> 1
Ex. 197: 221131 -> 1
                         Ex. 251: 231221 -> 0
                                                 Ex. 306: 3 1 1 3 1 2 -> 1
                         Ex. 252: 231222 -> 0
Ex. 198: 221132 -> 1
                         Ex. 253: 231231 -> 0
                                                 Ex. 307: 3 1 1 3 2 1 -> 1
Ex. 199: 221141 -> 0
Ex. 200: 221142 -> 0
                         Ex. 254: 231232 -> 0
                                                 Ex. 308: 311322 -> 1
                                                 Ex. 309: 3 1 1 3 3 1 -> 1
                         Ex. 255: 231241 -> 0
Ex. 201: 2 2 1 2 1 1 -> 1
                         Ex. 256: 231242 -> 0
                                                 Ex. 310: 311332 -> 1
Ex. 202: 221212 -> 1
                                                 Ex. 311: 3 1 1 3 4 1 -> 0
Ex. 203: 221221 -> 1
                         Ex. 257: 231311 -> 0
                                                 Ex. 312: 311342 -> 0
Ex. 204: 221222 -> 1
                         Ex. 258: 231312 -> 0
                                                 Ex. 313: 3 1 2 1 1 1 -> 1
                         Ex. 259: 231321 -> 0
Ex. 205: 221231 -> 1
                         Ex. 260: 231322 -> 0
                                                 Ex. 314: 312112 -> 1
Ex. 206: 221232 -> 1
Ex. 207: 2 2 1 2 4 1 -> 0
                         Ex. 261: 231331 -> 0
                                                 Ex. 315: 312121 -> 1
```

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Ex. 394: 331212 -> 0
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Ex. 316: 312122 -> 1
                                                    Ex. 395: 3 3 1 2 2 1 -> 0
                          Ex. 356: 321322 -> 1
Ex. 317: 312131 -> 1
                          Ex. 357: 321331 -> 1
                                                    Ex. 396: 3 3 1 2 2 2 -> 0
Ex. 318: 312132 -> 1
                                                    Ex. 397: 3 3 1 2 3 1 -> 0
                          Ex. 358: 321332 -> 1
Ex. 319: 312141 -> 0
                          Ex. 359: 321341 -> 0
                                                    Ex. 398: 3 3 1 2 3 2 -> 0
Ex. 320: 312142 -> 0
                                                    Ex. 399: 331241 -> 0
                          Ex. 360: 321342 -> 0
Ex. 321: 3 1 2 2 1 1 -> 1
                                                    Ex. 400: 331242 -> 0
                          Ex. 361: 3 2 2 1 1 1 -> 1
Ex. 322: 3 1 2 2 1 2 -> 1
                          Ex. 362: 3 2 2 1 1 2 -> 1
                                                    Ex. 401: 3 3 1 3 1 1 -> 0
Ex. 323: 312221 -> 1
                                                    Ex. 402: 3 3 1 3 1 2 -> 0
                          Ex. 363: 3 2 2 1 2 1 -> 1
Ex. 324: 312222 -> 1
                                                    Ex. 403: 3 3 1 3 2 1 -> 0
                          Ex. 364: 322122 -> 1
Ex. 325: 312231 -> 1
                          Ex. 365: 3 2 2 1 3 1 -> 1
                                                    Ex. 404: 331322 -> 0
Ex. 326: 3 1 2 2 3 2 -> 1
                          Ex. 366: 3 2 2 1 3 2 -> 1
                                                    Ex. 405: 331331 -> 0
Ex. 327: 312241 -> 0
Ex. 328: 312242 -> 0
                                                    Ex. 406: 331332 -> 0
                          Ex. 367: 3 2 2 1 4 1 -> 0
Ex. 329: 3 1 2 3 1 1 -> 1
                          Ex. 368: 322142 -> 0
                                                    Ex. 407: 331341 -> 0
                                                    Ex. 408: 331342 -> 0
                          Ex. 369: 322211 -> 1
Ex. 330: 312312 -> 1
                                                    Ex. 409: 332111 -> 0
                          Ex. 370: 3 2 2 2 1 2 -> 1
Ex. 331: 3 1 2 3 2 1 -> 1
Ex. 332: 3 1 2 3 2 2 -> 1
                          Ex. 371: 322221 -> 1
                                                    Ex. 410: 332112 -> 0
                                                    Ex. 411: 332121 -> 0
                          Ex. 372: 3 2 2 2 2 2 -> 1
Ex. 333: 3 1 2 3 3 1 -> 1
                                                    Ex. 412: 332122 -> 0
                          Ex. 373: 3 2 2 2 3 1 -> 1
Ex. 334: 312332 -> 1
                                                    Ex. 413: 332131 -> 1
                          Ex. 374: 322232 -> 1
Ex. 335: 312341 -> 0
                          Ex. 375: 322241 -> 0
                                                    Ex. 414: 332132 -> 1
Ex. 336: 312342 -> 0
                                                    Ex. 415: 332141 -> 0
                          Ex. 376: 322242 -> 0
Ex. 337: 3 2 1 1 1 1 -> 1
                                                    Ex. 416: 332142 -> 0
                          Ex. 377: 3 2 2 3 1 1 -> 1
Ex. 338: 3 2 1 1 1 2 -> 1
                                                    Ex. 417: 332211 -> 0
                          Ex. 378: 3 2 2 3 1 2 -> 1
Ex. 339: 3 2 1 1 2 1 -> 1
                          Ex. 379: 322321 -> 1
                                                    Ex. 418: 332212 -> 0
Ex. 340: 3 2 1 1 2 2 -> 1
                                                    Ex. 419: 332221 -> 0
                          Ex. 380: 322322 -> 1
Ex. 341: 3 2 1 1 3 1 -> 1
                                                    Ex. 420: 332222 -> 0
Ex. 342: 3 2 1 1 3 2 -> 1
                          Ex. 381: 322331 -> 1
                                                    Ex. 421: 332231 -> 0
                          Ex. 382: 3 2 2 3 3 2 -> 1
Ex. 343: 3 2 1 1 4 1 -> 0
                          Ex. 383: 322341 -> 0
                                                    Ex. 422: 332232 -> 0
Ex. 344: 3 2 1 1 4 2 -> 0
                                                    Ex. 423: 332241 -> 0
                          Ex. 384: 322342 -> 0
Ex. 345: 3 2 1 2 1 1 -> 1
                                                    Ex. 424: 332242 -> 0
                          Ex. 385: 3 3 1 1 1 1 -> 0
Ex. 346: 321212 -> 1
                                                    Ex. 425: 332311 -> 0
                          Ex. 386: 331112 -> 0
Ex. 347: 321221 -> 1
                          Ex. 387: 331121 -> 0
                                                    Ex. 426: 332312 -> 0
Ex. 348: 321222 -> 1
                                                    Ex. 427: 332321 -> 0
                          Ex. 388: 331122 -> 0
Ex. 349: 3 2 1 2 3 1 -> 1
                          Ex. 389: 331131 -> 1
                                                    Ex. 428: 332322 -> 0
Ex. 350: 3 2 1 2 3 2 -> 1
                          Ex. 390: 331132 -> 1
                                                    Ex. 429: 332331 -> 0
Ex. 351: 321241 -> 0
                                                    Ex. 430: 332332 -> 0
                          Ex. 391: 331141 -> 0
Ex. 352: 3 2 1 2 4 2 -> 0
Ex. 353: 3 2 1 3 1 1 -> 1
                                                    Ex. 431: 332341 -> 0
                          Ex. 392: 3 3 1 1 4 2 -> 0
                          Ex. 393: 331211 -> 0
                                                    Ex. 432: 332342 -> 0
Ex. 354: 3 2 1 3 1 2 -> 1
```